



# RIF RDF and OWL Compatibility

W3C Editor's Draft 29 September 2009

**This version:**

<http://www.w3.org/2005/rules/wg/draft/ED-rif-rdf-owl-20090929/>

**Latest editor's draft:**

<http://www.w3.org/2005/rules/wg/draft/rif-rdf-owl/>

**Previous version:**

<http://www.w3.org/2005/rules/wg/draft/ED-rif-rdf-owl-20090904/> ([color-coded diff](#))

**Editors:**

Jos de Bruijn, Free University of Bozen/Bolzano

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## Abstract

Rules interchanged using the Rule Interchange Format RIF may depend on or be used in combination with RDF data and RDF Schema or OWL ontologies. This document, developed by the [Rule Interchange Format \(RIF\) Working Group](#), specifies the interoperation between RIF and the data and ontology languages RDF, RDF Schema, and OWL.

## Status of this Document

### May Be Superseded

*This section describes the status of this document at the time of its publication. Other documents may supersede this document. A list of current W3C publications and the latest revision of this technical report can be found in the [W3C technical reports index](#) at <http://www.w3.org/TR/>.*

## Set of Documents

This document is being published as one of a set of 10 documents:

1. [RIF Overview](#)
2. [RIF Core Dialect](#)
3. [RIF Basic Logic Dialect](#)
4. [RIF Framework for Logic Dialects](#)
5. [RIF RDF and OWL Compatibility](#) (this document)
6. [RIF Datatypes and Built-Ins 1.0](#)
7. [RIF Production Rule Dialect](#)
8. [RIF Test Cases](#)
9. [RIF Combination with XML data](#)
10. [OWL 2 RL in RIF](#)

## Summary of Changes

There have been no [substantive](#) changes since the [previous version](#). For details on the minor changes see the [change log](#) and [color-coded diff](#).

## Please Comment By 27 October 2009

The [Rule Interchange Format \(RIF\) Working Group](#) seeks to gather experience from [implementations](#) in order to increase confidence in the language and meet specific [exit criteria](#). This document will remain a Candidate Recommendation until at least 27 October 2009. After that date, when and if the exit criteria are met, the group intends to request [Proposed Recommendation](#) status.

Please send reports of implementation experience, and other feedback, to [public-rif-comments@w3.org](mailto:public-rif-comments@w3.org) ([public archive](#)). Reports of any success or difficulty with the [test cases](#) are encouraged. Open discussion among developers is welcome at [public-rif-dev@w3.org](mailto:public-rif-dev@w3.org) ([public archive](#)).

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## 1 Overview of RDF and OWL Compatibility

The Rule Interchange Format (RIF) is a format for interchanging rules over the Web. Rules that are exchanged using RIF may refer to external data sources and may be based on data models that are represented using a language different from RIF. The Resource Description Framework [RDF](#) [[RDF-Concepts](#)] is a Web-based language for the representation and exchange of data; [RDF Schema](#) (RDFS) [[RDF-Schema](#)] and the [OWL](#) Web Ontology Language [[OWL2-Syntax](#)] are Web-based languages for representing and exchanging ontologies. This document specifies how combinations of RIF documents and RDF data and RDFS and OWL ontologies are interpreted; i.e., it specifies how RIF interoperates with RDF, RDFS, and OWL. We consider here OWL 2 [[OWL2-Syntax](#)], which is an extension of OWL 1 [[OWL-Reference](#)]. Therefore, the notions defined in this document also apply to combinations of RIF documents with OWL 1 ontologies.

We consider here the RIF Basic Logic Dialect (BLD) [[RIF-BLD](#)] and RIF Core [[RIF-Core](#)], a subset of RIF BLD. The RIF Production Rule Dialect (PRD) [[RIF-PRD](#)] is an extension of RIF Core. Interoperability between RIF and RDF/OWL is only defined for the Core subset of PRD. In the remainder, when speaking about RIF documents and rules, we refer to RIF Core and BLD.

RDF data and RDFS and OWL ontologies can be represented using *RDF graphs*. There exist several alternative syntaxes for OWL ontologies; however, for exchange purposes it is assumed they are represented using RDF graphs.

Several syntaxes have been proposed for the exchange of RDF graphs, the normative syntax being RDF/XML [[RDF-Syntax](#)]. RIF does not provide a format for exchanging RDF graphs; it is assumed that RDF graphs are exchanged using RDF/XML, or any other syntax that can be used for representing or exchanging RDF graphs.

A typical scenario for the use of RIF with RDF/OWL is the exchange of rules that use RDF data and/or RDFS or OWL ontologies: an interchange partner *A* has a rules language that is RDF/OWL-aware, i.e., it supports the use of RDF data, it uses an RDFS or OWL ontology, or it extends RDF(S)/OWL. *A* sends its rules using RIF, possibly with references to the appropriate RDF graph(s), to partner *B*.

*B* receives the rules and retrieves the referenced RDF graph(s). The rules are translated to the internal rules language of *B* and are processed, together with the RDF graphs, using the RDF/OWL-aware rule engine of *B*. The use case [Vocabulary Mapping for Data Integration \[RIF-UCR\]](#) is an example of the interchange of RIF rules that use RDF data and RDFS ontologies.

A specialization of this scenario is the publication of RIF rules that refer to RDF graphs; publication is a special kind of interchange: one to many, rather than one-to-one. When a rule publisher *A* publishes its rules on the Web, there may be several consumers that retrieve the RIF rules and RDF graphs from the Web, translate the RIF rules to their respective rules languages, and process them together with the RDF graphs in their own rules engines. The use case [Publishing Rules for Interlinked Metadata \[RIF-UCR\]](#) illustrates the publication scenario.

Another specialization of the exchange scenario is the [Interchange of Rule Extensions to OWL \[RIF-UCR\]](#). The intention of the rule publisher in this scenario is to extend an OWL ontology with rules: interchange partner *A* has a rules language that extends OWL. *A* splits its ontology+rules description into a separate OWL ontology and a RIF document, publishes the OWL ontology, and sends (or publishes) the RIF document, which includes a reference to the OWL ontology. A consumer of the rules retrieves the OWL ontology and translates the ontology and document into a combined ontology+rules description in its own rule extension of OWL.

A RIF document that refers to (*imports*) RDF graphs and/or RDFS/OWL ontologies, or any use of a RIF document with RDF graphs, is viewed as a combination of a document and a number of graphs and ontologies. This document specifies how, in such a combination, the document and the graphs and ontologies interoperate in a technical sense, i.e., the conditions under which the combination is satisfiable (i.e., consistent), as well as the entailments (i.e., logical consequences) of the combination. The interaction between RIF and RDF/OWL is realized by connecting the model theory of RIF [[RIF-BLD](#)] with the model theories of RDF [[RDF-Semantics](#)] and OWL [[OWL2-Semantics](#)], respectively.

The notation of certain symbols in RIF, particularly IRIs and plain literals, is slightly different from the notation in RDF/OWL. These differences are illustrated in the Section [Symbols in RIF Versus RDF/OWL](#).

The RDF semantics specification [[RDF-Semantics](#)] defines four normative notions of entailment for RDF graphs: Simple, RDF, RDFS, and Datatype entailment. OWL 2 specifies two different semantics, with corresponding notions of entailment: the direct semantics [[OWL2-Semantics](#)], which specifies OWL 2 DL entailment, and the RDF-based semantics [[OWL2-RDF-Based-Semantics](#)], which specifies OWL 2 Full entailment. This document specifies the interaction between RIF and RDF/OWL for all six notions. The Section [RDF Compatibility](#) is concerned with the combination of RIF and RDF/RDFS. The combination of RIF and OWL is addressed in the Section

[OWL Compatibility](#). The semantics of the interaction between RIF and OWL 2 DL is close in spirit to [\[SWRL\]](#).

RIF provides a mechanism for referring to (importing) RDF graphs and a means for specifying the *profile* of this import, which corresponds to the intended entailment regime. The Section [Importing RDF and OWL in RIF](#) specifies how such import statements are used for representing RIF-RDF and RIF-OWL combinations.

The [Appendix: Embeddings \(Informative\)](#) describes how reasoning with combinations of RIF rules with RDF and OWL 2 RL (a subset of OWL 2 DL) can be reduced to reasoning with RIF documents. This reduction can be seen as an implementation hint for interchange partners who do not have RDF/OWL-aware rule systems, but want to process RIF rules that import RDF graphs and OWL ontologies. In terms of the aforementioned scenario: if the interchange partner *B* does not have an RDF/OWL-aware rule system, but *B* can process RIF rules, then the appendix explains how the rule system of *B* could be used for processing RIF-RDF/OWL combinations.

Throughout this document the following conventions are used when writing RIF and RDF statements in examples and definitions.

- All RIF statements are written using the [RIF presentation syntax \[RIF-BLD\]](#). Where possible, this document uses the [shortcut syntax for IRIs and strings](#) as defined in [\[RIF-DTB\]](#).
- RDF triples are written using the Turtle syntax [\[Turtle\]](#): triples are written as *s p o*, where *s*, *p*, and *o* are blank nodes `_:x`, IRIs delimited with '<' and '>', compact IRIs `prefix:localname`, plain literals without language tags `"literal"`, plain literals with language tags `"literal"@lang`, or typed literals `"literal"^^datatype-IRI`.
- The following namespace prefixes are used throughout this document: *ex* refers to `http://example.org/example#`, *xs* refers to `http://www.w3.org/2001/XMLSchema#`, *rdf* refers to `http://www.w3.org/1999/02/22-rdf-syntax-ns#`, *rdfs* refers to `http://www.w3.org/2000/01/rdf-schema#`, *owl* refers to `http://www.w3.org/2002/07/owl#`, and *rif* refers to `http://www.w3.org/2007/rif#`.

## 2 Symbols in RIF versus RDF/OWL (Informative)

Where RDF/OWL has four kinds of constants: [URI references](#) (i.e., IRIs), [plain literals without language tags](#), [plain literals with language tags](#) and [typed literals](#) (i.e., Unicode sequences with datatype IRIs) [\[RDF-Concepts\]](#), RIF has one kind of constants: Unicode sequences with symbol space IRIs [\[RIF-DTB\]](#).

[Symbol spaces](#) can be seen as groups of constants. Every datatype is a symbol space, but there are symbol spaces that are not datatypes. For example, the

symbol space `rif:iri` groups all IRIs. The correspondence between constant symbols in RDF graphs and RIF documents is explained in [Table 1](#).

Table 1. Correspondence between RDF and RIF symbols.

RDF Symbol	Example	RIF Symbol	Example
IRI	<code>&lt;http://www.w3.org/2007/rif&gt;</code>	Constant in the <code>rif:iri</code> symbol space	<code>"http://www.w3.org/2007/rif"^^rif:iri</code>
Plain literal without language tag	<code>"literal string"</code>	Constant in the <code>xs:string</code> symbol space	<code>"literal string"^^xs:string</code>
Plain literal with language tag	<code>"literal string"@en</code>	Constant in the <code>rdf:PlainLiteral</code> symbol space	<code>"literal string"@en"^^rdf:PlainLiteral</code>
Typed literal	<code>"1"^^xs:integer</code>	Constant with symbol space	<code>"1"^^xs:integer</code>

The [shortcut syntax for IRIs and strings \[RIF-DTB\]](#), used throughout this document, corresponds to the syntax for IRIs and plain literals in Turtle [\[Turtle\]](#), a commonly used syntax for RDF.

- IRIs, i.e., constants of the form `"IRI"^^rif:iri`, may be written as `<IRI>` or as compact IRIs [\[CURIE\]](#), i.e., as `prefix:localname`, where `prefix` is understood to refer to an IRI `namespace-IRI`, and `prefix:localname` stands for the IRI (`IRI`) obtained by concatenating `namespace-IRI` and `localname`.
- Strings, i.e., constants of the form `"my string"^^xs:string` may be written as `"my string"`.

RIF does not have a notion corresponding exactly to RDF [blank nodes](#). RIF [local symbols](#), written `_symbolname`, have some commonality with blank nodes; like the blank node label, the name of a local symbol is not exposed outside of the document. However, in contrast to blank nodes, which are essentially existentially quantified variables, RIF local symbols are *constant* symbols. In many applications and deployment scenarios, this difference may be inconsequential. However the results will differ when such symbols are used in a non-assertional context, such as in a query pattern or rule body.

Finally, [variables](#) in the bodies of RIF rules or in query patterns may be existentially quantified, and are thus similar to blank nodes; however, RIF BLD does not allow existentially quantified variables to occur in rule heads.

### 3 RDF Compatibility

This section specifies how a RIF document interacts with a set of RDF graphs in a RIF-RDF combination. In other words, how rules can "access" data in the RDF graphs.

There is a correspondence between statements in RDF graphs and certain kinds of formulas in RIF. Namely, there is a correspondence between RDF triples of the form  $s \ p \ o$  and RIF frame formulas of the form  $s' [p' \ -> \ o']$ , where  $s'$ ,  $p'$ , and  $o'$  are RIF symbols corresponding to the RDF symbols  $s$ ,  $p$ , and  $o$ , respectively. This means that whenever a triple  $s \ p \ o$  is satisfied, the corresponding RIF frame formula  $s' [p' \ -> \ o']$  is satisfied, and vice versa.

Consider, for example, a combination of an RDF graph that contains the triples

```
ex:john ex:brotherOf ex:jack .
ex:jack ex:parentOf ex:mary .
```

saying that `ex:john` is a brother of `ex:jack` and `ex:jack` is a parent of `ex:mary`, and a RIF document that contains the rule

```
forall ?x ?y ?z (?x[ex:uncleOf -> ?z] :-
  And(?x[ex:brotherOf -> ?y] ?y[ex:parentOf -> ?z]))
```

which says that whenever some  $x$  is a brother of some  $y$  and  $y$  is a parent of some  $z$ , then  $x$  is an uncle of  $z$ . From this combination the RIF frame formula `:john[:uncleOf -> :mary]`, as well as the RDF triple `:john :uncleOf :mary`, are consequences of this combination.

Note that blank nodes cannot be referenced directly from RIF rules, since blank nodes are local to a specific RDF graph. Variables in RIF rules do, however, range over objects denoted by blank nodes. So, it is possible to "access" an object denoted by a blank node from a RIF rule using a variable in a rule.

The following example illustrates the interaction between RDF and RIF in the face of blank nodes.

Consider a combination of an RDF graph that contains the triple

```
_:x ex:hasName "John" .
```

saying that there is something, denoted here by a blank node, which has the name "John", and a RIF document that contains the rules

```

Forall ?x ?y ( ?x[rdf:type -> ex:named] :- ?x[ex:hasName -> ?y] )
Forall ?x ?y ( <http://a>[<http://p> -> ?y] :- ?x[ex:hasName -> ?y] )

```

which says that whenever there is some  $x$  that has some name  $y$ , then  $x$  is of type `ex:named` and `http://a` has a property `http://p` with value  $y$ .

From this combination the following RIF condition formulas can be derived:

```

Exists ?z (?z[rdf:type -> ex:named])
<http://a>[<http://p> -> "John"]

```

as can the following RDF triples:

```

_:y rdf:type ex:named .
<http://a> <http://p> "John" .

```

However, there is no RIF constant symbol  $t$  such that `t[rdf:type -> ex:named]` can be derived, because there is no constant that represents the named individual.

Note that, even when considering [Simple entailment](#), not every combination is satisfiable. In fact, not every RIF document has a model. For example, the RIF BLD document consisting of the fact

```
"a"="b"
```

does not have a model, since the symbols "a" and "b" are mapped to the (distinct) character strings "a" and "b", respectively, in every semantic structure.

One consequence of the difference of the alphabets of RDF and RIF is that IRIs of the form `http://iri` and typed literals of the form `"http://iri"^^rif:iri` that occur in an RDF graph are treated the same in RIF-RDF combinations, even if the RIF document is empty. However, documents importing RDF graphs containing typed literals of the form `"http://iri"^^rif:iri` must be rejected.

Plain literals without language tags of the form `"mystring"` and typed literals of the form `"mystring"^^xs:string` also correspond. For example, consider the combination of an empty document and an RDF graph that contains the triple

```
<http://a> <http://p> "abc" .
```

This combination entails, among other things, the following frame formula:

```
<http://a>[<http://p> -> "abc"^^xs:string]
```

as well as the following triple:

```
<http://a> <http://p> "abc"^^xs:string .
```

These entailments are sanctioned by the semantics of plain literals and `xs:stringS`.

Lists in RDF (also called [collections](#)) have a natural correspondence to RIF lists. For example, the RDF list `_:l1 rdf:first ex:b . _:l1 rdf:rest rdf:nil .` corresponds to the RIF list `List(ex:b)`. And so, the combination of the empty RIF document with the RDF graph

```
ex:a ex:p _:l1 .
_:l1 rdf:first ex:b .
_:l1 rdf:rest rdf:nil .
```

entails the formula

```
ex:a[ex:p -> List(ex:b)].
```

Likewise, the combination of the empty RDF graph with the RIF fact

```
ex:p(List(ex:a))
```

entails the triples

```
_:l1 rdf:first ex:a .
_:l1 rdf:rest rdf:nil .
```

as well as the formula

```
Exists ?x (And(ex:p(?x) ?x[rdf:first -> ex:a] ?x[rdf:rest -> rdf:nil])).
```

**Editor's Note:** This last example shows there is a 1-to-1 correspondence between RIF and RDF lists. Note that 1-to-1 correspondence (condition 10 in [common-RIF-RDF-interpretations](#)) is at risk. The previous example shows that RIF lists extend RDF lists (condition 9 in [common-RIF-RDF-interpretations](#)); this feature is not at risk.

The remainder of this section formally defines combinations of RIF rules with RDF graphs and the semantics of such combinations. A combination consists of a RIF document and a set of RDF graphs. The semantics of combinations is defined in terms of combined models, which are pairs of RIF and RDF interpretations. The interaction between the two interpretations is defined through a number of conditions. Entailment is defined as model inclusion, as usual.

### 3.1 Syntax of RIF-RDF Combinations

This section first reviews the definitions of RDF vocabularies and RDF graphs, after which RIF-RDF combinations are formally defined. The section concludes with a review of definitions related to datatypes and typed literals.

#### 3.1.1 RDF Vocabularies and Graphs

An RDF [vocabulary](#)  $V$  consists of the following sets of *names*:

- [IRIs](#)  $V_U$ , (corresponds to the Concepts and Abstract Syntax term "[RDF URI references](#)"; see the [End note on RDF URI references](#))
- [plain literals](#)  $V_{PL}$  (i.e., character strings with an optional language tag), and
- [typed literals](#)  $V_{TL}$  (i.e., pairs of character strings and datatype IRIs).

In addition, there is an infinite set of [blank nodes](#), which is disjoint from the sets of names. See [RDF Concepts and Abstract Syntax \[RDF-Concepts\]](#) for precise definitions of these concepts.

**Definition.** Given an RDF vocabulary  $V$ , a **generalized RDF triple** of  $V$  is a statement of the form  $s \ p \ o$ , where  $s$ ,  $p$  and  $o$  are names in  $V$  or blank nodes.  $\square$

**Definition.** Given an RDF vocabulary  $V$ , a **generalized RDF graph** is a set of **generalized RDF triples** of  $V$ .  $\square$

(See the [End note on generalized RDF graphs](#))

#### 3.1.2 RIF-RDF Combinations

A RIF-RDF combination consists of a RIF document and zero or more RDF graphs. Formally:

**Definition.** A **RIF-RDF combination** is a pair  $\langle R, \mathbf{S} \rangle$ , where  $R$  is a [RIF document](#) and  $\mathbf{S}$  is a set of [generalized RDF graphs](#) of a vocabulary  $V$ .  $\square$

When clear from the context, RIF-RDF combinations are referred to simply as **combinations**.

#### 3.1.3 Datatypes and Typed Literals

Even though RDF allows the use of arbitrary datatype IRIs in typed literals, not all such datatype IRIs are recognized in the semantics. In fact, Simple entailment does not recognize any datatype and RDF and RDFS entailment recognize only the datatype [rdf:XMLLiteral](#). To facilitate discussing datatypes, and specifically

datatypes supported in specific contexts (required for RIF-D-entailment), the notion of datatype maps [[RDF-Semantics](#)] is used.

A [datatype map](#) is a partial mapping from IRIs to [datatypes](#).

RDFS, specifically RIF-D-entailment, allows the use of arbitrary datatype maps, as long as `rdf:XMLLiteral` is in the domain of the map. RIF BLD requires a number of additional datatypes to be included; these are the [RIF-required datatypes](#) [[RIF-DTB](#)].

When checking consistency of a [combination](#)  $\langle R, \mathbf{S} \rangle$  or entailment of a graph  $S$  or RIF formula  $\varphi$  by a combination  $\langle R, \mathbf{S} \rangle$ , the set of **considered datatypes** is the union of the set of [RIF-required datatypes](#) and the sets of datatypes referenced in  $R$ , the documents [imported into](#)  $R$ , and  $\varphi$  (when considering entailment of  $\varphi$ ).

**Definition.** Let DTS be a set of [datatypes](#). A [datatype map](#)  $D$  is **conforming** with DTS if it satisfies the following conditions:

1. Every IRI identifying a datatypes in DTS is in the domain of  $D$ .
  2.  $D$  maps each IRI in its domain to the datatype in identified by that IRI in T.
- 

Note that it follows from the definition that every datatype used in the RIF document in the combination or the entailed RIF formula (when considering entailment questions) is included in any datatype map conforming to the set of considered datatypes. There may be datatypes used in an RDF graph in the combination that are not included in such a datatype map.

**Definition.** Given a datatype map  $D$ , a typed literal  $(s, d)$  is a **well-typed literal** if

1.  $d$  is in the domain of  $D$  and  $s$  is in the lexical space of  $D(d)$  or
2.  $d$  is the IRI of a [symbol space](#) required by RIF BLD and  $s$  is in the lexical space of the symbol space. □

### 3.2 Semantics of RIF-RDF Combinations

The semantics of RIF-RDF combinations is defined through a combination of the RIF and RDF model theories, using a notion of *common models*. These models are then used to define satisfiability and entailment in the usual way. Combined entailment extends both entailment in RIF and entailment in RDF.

The RDF Semantics document [[RDF-Semantics](#)] defines four normative kinds of interpretations, as well as corresponding notions of satisfiability and entailment:

- [Simple interpretations](#), which do not impose any conditions on the RDF and RDFS vocabularies,
- [RDF interpretations](#), which impose additional conditions on the interpretation of the RDF vocabulary,

- [RDFS interpretations](#), which impose additional conditions on the interpretation of the RDF and RDFS vocabularies, and
- [D-interpretations](#), which impose additional conditions on the treatment of datatypes, relative to a [datatype map](#) D.

Those four types of interpretations are reflected in the definitions of satisfaction and entailment in this section.

### 3.2.1 Interpretations

This section defines the notion of *common-RIF-RDF-interpretation*, which is an interpretation of a RIF-RDF combination. This common-RIF-RDF-interpretation is the basis for the definitions of satisfaction and entailment in the following sections.

The correspondence between [RIF semantic structures](#) (interpretations) and [RDF interpretations](#) is defined through a number of conditions that ensure the correspondence in the interpretation of names (i.e., IRIs and literals) and formulas, i.e., the correspondence between RDF triples of the form  $s \ p \ o$  and RIF frames of the form  $s' \ [p' \ \rightarrow \ o']$ , where  $s'$ ,  $p'$ , and  $o'$  are RIF symbols corresponding to the RDF symbols  $s$ ,  $p$ , and  $o$ , respectively (cf. the Section [Symbols in RIF Versus RDF/OWL](#)).

#### 3.2.1.1 RDF and RIF Interpretations

The notions of RDF interpretation and RIF semantic structure (interpretation) are briefly reviewed below.

As defined in [\[RDF-Semantics\]](#), a [Simple interpretation](#) of a vocabulary  $V$  is a tuple  $I = \langle IR, IP, IEXT, IS, IL, LV \rangle$ , where

- IR is a non-empty set of resources (the domain),
- IP is a set of properties,
- IEXT is an extension function, which is a mapping from IP into the power set of  $IR \times IR$ ,
- IS is a mapping from IRIs in  $V$  into  $(IR \cup IP)$ ,
- IL is a mapping from typed literals in  $V$  into IR, and
- LV is the set of literal values, which is a subset of IR, and includes all plain literals in  $V$ .

RDF-, RDFS-, and D-interpretations are Simple interpretations that satisfy certain conditions:

- A Simple interpretation  $I$  of a vocabulary  $V$  is an [RDF-interpretation](#) if  $V$  includes the [RDF vocabulary](#) and  $I$  satisfies the [RDF axiomatic triples](#) and the [RDF semantic conditions](#).
- An RDF-interpretation  $I$  of a vocabulary  $V$  is an [RDFS-interpretation](#) if  $V$  includes the RDFS vocabulary and  $I$  satisfies the [RDFS axiomatic triples](#) and the [RDFS semantic conditions](#).

- Given a datatype map  $D$ , an RDFS-interpretation  $I$  of a vocabulary  $V$  is a ***D*-interpretation** if  $V$  includes the IRIs in the domain of  $D$  and  $I$  satisfies the **general semantic conditions for datatypes** for every pair  $\langle d, D(d) \rangle$  such that  $d$  is in the domain of  $D$ .

As defined in [RIF-BLD], a **semantic structure**  $I$  is a tuple of the form  $\langle TV, DTS, D, D_{ind}, D_{func}, I_C, I_V, I_F, I_{NF}, I_{list}, I_{tail}, I_{frame}, I_{sub}, I_{isa}, I_=, I_{external}, I_{truth} \rangle$ . The specification of RIF-RDF compatibility is only concerned with  $DTS, D, I_C, I_V, I_{list}, I_{tail}, I_{frame}, I_{sub}, I_{isa}$ , and  $I_{truth}$ . The other mappings that are parts of a semantic structure are not used in the definition of combinations.

Recall that  $Const$  is the set of **constant symbols** and  $Var$  is the set of **variable symbols** in RIF.

- $DTS$  is the set of datatypes, which have associated datatype identifiers,
- $D$  is a set (the domain),
- $D_{ind}$  is a non-empty subset of  $D$ ,
- $D_{func}$  is a non-empty subset of  $D$ ,
- $I_C$  is a mapping from constants to  $D$  such that constants in individual position are mapped to  $D_{ind}$  and constants in function positions are mapped to  $D_{func}$ ,
- $I_V$  is a mapping from  $Var$  to  $D_{ind}$ ,
- $I_{list}$  is an injective mapping from  $D_{ind}^*$  to  $D_{ind}$ ,
- $I_{tail}$  is a mapping from  $D_{ind}^+ \times D_{ind}$  to  $D_{ind}$ ,
- $I_{frame}$  is a mapping from  $D_{ind}$  to functions of the form  $SetOfFiniteBags(D_{ind} \times D_{ind}) \rightarrow D$ ,
- $I_{sub}$  is a mapping from  $D_{ind} \times D_{ind}$  to  $D$ ,
- $I_{isa}$  is a mapping from  $D_{ind} \times D_{ind}$  to  $D$ , and
- $I_{truth}$  is a mapping from  $D$  to  $TV$ .

For the purpose of the interpretation of imported documents, RIF BLD defines the notion of **semantic multi-structures**, which are nonempty sets of semantic structures of the form  $\{J, I, I^1, I^2, \dots\}$  that differ only in interpretation of local constants. The structure  $I$  in the above is used to interpret document formulas, and will be used to specify RIF combinations.

### 3.2.1.2 RDF Lists

Syntactically speaking, an RDF list is a set of triples of the form

```
i1 rdf:first d1 .
i1 rdf:rest i2 .
...
in rdf:first dn .
in rdf:rest rdf:nil .
```

Here,  $i_1 \dots i_n$  provide the structure of the linked list and  $d_1 \dots d_n$  are the items. The above list would be written in RIF syntax as `List(d1 ... dn)`.

Given an RDF interpretation  $I = \langle IR, IP, IEXT, IS, IL, LV \rangle$ , we say that an element  $l_1 \in IR$  refers to an **RDF list**  $(y_1, \dots, y_n)$  if  $l_1 = IS(\text{rdf:nil})$ , in case  $n=0$ ; otherwise,  $\exists l_2, \dots, l_n$  such that  $\langle l_1, y_1 \rangle \in IEXT(IS(\text{rdf:first}))$ ,  $\langle l_1, l_2 \rangle \in IEXT(IS(\text{rdf:rest}))$ , ...,  $\langle l_n, y_n \rangle \in IEXT(IS(\text{rdf:first}))$ , and  $\langle l_n, IS(\text{rdf:nil}) \rangle \in IEXT(IS(\text{rdf:rest}))$ .

Note that, if  $n > 0$ , there may be several lists referred to by  $l_1$ , since there is no restriction, in general, on the `rdf:first` elements and the `rdf:rest` successors.

### 3.2.1.3 Common RIF-RDF Interpretations

**Definition.** A **common-RIF-RDF-interpretation** is a pair  $(\hat{I}, I)$ , where  $\hat{I}$  is a [semantic multi-structure](#) of the form  $\{J, I; I^{i_1}, I^{i_2}, \dots\}$ , and  $I$  is a [Simple interpretation](#) of a vocabulary  $V$ , such that the following conditions hold:

1.  $(IR \text{ union } IP) = D_{\text{ind}}$ ;
2.  $IP$  is a superset of the set of all  $k$  in  $D_{\text{ind}}$  such that there exist some  $a, b$  in  $D_{\text{ind}}$  and  $I_{\text{truth}}(I_{\text{frame}}(a)(k,b)) = \text{t}$ ;
3.  $LV$  is a superset of (union of the value spaces of all [considered datatypes](#));
4.  $IEXT(k) =$  the set of all pairs  $(a, b)$ , with  $a, b$ , and  $k$  in  $D_{\text{ind}}$ , such that  $I_{\text{truth}}(I_{\text{frame}}(a)(k,b)) = \text{t}$ ;
5.  $IS(i) = IC(\langle i \rangle)$  for every IRI  $i$  in  $VU$ ;
6.  $IL((s, d)) = IC("s" \wedge d)$  for every [well-typed literal](#)  $(s, d)$  in  $VTL$ ;
7.  $IEXT(IS(\text{rdf:type}))$  is equal to the set of all pairs  $(a, b)$  in  $D_{\text{ind}} \times D_{\text{ind}}$  such that  $I_{\text{truth}}(I_{\text{isa}}(a,b)) = \text{t}$ ; and
8.  $IEXT(IS(\text{rdfs:subClassOf}))$  is a superset of the set of all pairs  $(a, b)$  in  $D_{\text{ind}} \times D_{\text{ind}}$  such that  $I_{\text{truth}}(I_{\text{sub}}(a,b)) = \text{t}$ ;
9. For any nonnegative integer  $n$  and any  $y_1, \dots, y_n \in IR$ , if some  $l_1 \in IR$  refers to the [RDF list](#)  $(y_1, \dots, y_n)$ , then  $I_{\text{list}}(y_1, \dots, y_n) = l_1$ ; and
10. For any nonnegative integer  $n$  and any sequence of elements  $y_1, \dots, y_n \in IR$ , an element  $l_1 \in IR$  refers to the [RDF list](#)  $(y_1, \dots, y_n)$  iff  $I_{\text{list}}(y_1, \dots, y_n) = l_1$ .  $\square$

Condition 1 ensures that the combination of resources and properties corresponds exactly to the RIF domain; note that if  $I$  is an RDF-, RDFS-, or D-interpretation,  $IP$  is a subset of  $IR$ , and thus  $IR = D_{\text{ind}}$ . Condition 2 ensures that the set of RDF properties at least includes all elements that are used as properties in frames in the RIF domain. Condition 3 ensures that all concrete values in  $D_{\text{ind}}$  are included in  $LV$  (by definition, the value spaces of all considered datatypes are included in  $D_{\text{ind}}$ ). Condition 4 ensures that RDF triples are interpreted in the same way as frame formulas. Condition 5 ensures that IRIs are interpreted in the same way. Condition 6 ensures that typed literals are interpreted in the same way. Note that no correspondences are defined for the mapping of names in RDF that are not symbols of RIF, e.g., ill-typed literals and RDF URI references that are not absolute IRIs. Condition 7 ensures that typing in RDF and typing in RIF correspond, i.e., a

`rdf:type b` is true iff `a # b` is true. Condition 8 ensures that whenever a RIF subclass statement holds, the corresponding RDF subclass statement holds as well, i.e., a `rdfs:subClassOf b` is true if `a ## b` is true. Finally, condition 9 requires the existence of an RIF list for every RDF list and condition 10 in addition requires the existence of an RDF list for every RIF list.

#### Feature At Risk #1: 1-to-1 lists

*Note: This feature is "at risk" and may be removed from this specification based on feedback. Please send feedback to [public-rif-comments@w3.org](mailto:public-rif-comments@w3.org).*

Condition 10 (which implies condition 9), which ensures a one-to-one correspondence between RDF and RIF lists, is **AT RISK** and may be removed based on implementation experience.

### 3.2.2 Satisfaction and Models

The notion of satisfiability refers to the conditions under which a common-RIF-RDF-interpretation  $(\hat{I}, I)$  is a model of a combination  $\langle R, \mathbf{S} \rangle$ . The notion of satisfiability is defined for all four entailment regimes of RDF (i.e., Simple, RDF, RDFS, and D). The definitions are all analogous. Intuitively, a common-RIF-RDF-interpretation  $(\hat{I}, I)$  satisfies a combination  $\langle R, \mathbf{S} \rangle$  if  $\hat{I}$  is a model of  $R$  and  $I$  satisfies  $\mathbf{S}$ . Formally:

**Definition.** A [common-RIF-RDF-interpretation](#)  $(\hat{I}, I)$  *satisfies* a [RIF-RDF combination](#)  $C = \langle R, \mathbf{S} \rangle$  if  $\hat{I}$  is a [model](#) of  $R$  and  $I$  [satisfies](#) every RDF graph  $S$  in  $\mathbf{S}$ ; in this case  $(\hat{I}, I)$  is called a **RIF-Simple-model**, or **model**, of  $C$ , and  $C$  is **satisfiable**.  $(\hat{I}, I)$  satisfies a [generalized RDF graph](#)  $S$  if  $I$  satisfies  $S$ .  $(\hat{I}, I)$  satisfies a [condition formula](#)  $\varphi$  if  $TVal(\varphi) = t$ .  $\square$

Rdf-, RDFS-, and RIF-D-satisfiability are defined through additional restrictions on  $I$ :

**Definition.** A [model](#)  $(\hat{I}, I)$  of a combination  $C$  is an **RIF-RDF-model** of  $C$  if  $I$  is an [RDF-interpretation](#); in this case  $C$  is **RIF-RDF-satisfiable**.

A [model](#)  $(\hat{I}, I)$  of a combination  $C$  is an **RIF-RDFS-model** of  $C$  if  $I$  is an [RDFS-interpretation](#); in this case  $C$  is **RIF-RDFS-satisfiable**.

Let  $(\hat{I}, I)$  be a [model](#) of a combination  $C$  and let  $D$  be a datatype map [conforming](#) with the set **DTS** of datatypes in  $I$ .  $(\hat{I}, I)$  is a **RIF-D-model** of  $C$  if  $I$  is a [D-interpretation](#); in this case  $C$  is **RIF-D-satisfiable**.  $\square$

### 3.2.3 Entailment

Using the notions of models defined above, entailment is defined in the usual way, i.e., through inclusion of sets of models.

**Definition.** Let  $C$  be a RIF-RDF combination, let  $S$  be a [generalized RDF graph](#), let  $\varphi$  be a [condition formula](#), and let  $D$  be a datatype map [conforming](#) with the set of [considered datatypes](#).  $C$  **RIF-D-entails**  $S$  if every [RIF-D-model](#) of  $C$  [satisfies](#)  $S$ . Likewise,  $C$  **RIF-D-entails**  $\varphi$  if every [RIF-D-model](#) of  $C$  [satisfies](#)  $\varphi$ .  $\square$

The other notions of entailment are defined analogously:

**Definition.** A combination  $C$  **RIF-Simple-entails**  $S$  (resp.,  $\varphi$ ) if every [Simple model](#) of  $C$  [satisfies](#)  $S$  (resp.,  $\varphi$ ).

A combination  $C$  **RIF-RDF-entails**  $S$  (resp.,  $\varphi$ ) if every [RIF-RDF-model](#) of  $C$  [satisfies](#)  $S$  (resp.,  $\varphi$ ).

A combination  $C$  **RIF-RDFS-entails**  $S$  (resp.,  $\varphi$ ) if every [RIF-RDFS-model](#) of  $C$  [satisfies](#)  $S$  (resp.,  $\varphi$ ).  $\square$

Note that simple entailment in combination with an empty ruleset is not the same as simple entailment in RDF, since certain entailments involving datatypes are enforced by the RIF semantics in combinations, cf. the [example](#) involving strings and plain literals above.

## 4 OWL Compatibility

This section specifies how a RIF document interacts with a set of OWL ontologies in a RIF-OWL combination. The semantics of combinations is defined for OWL 2 [[OWL2-Syntax](#)]. Since OWL 2 is an extension of OWL 1 [[OWL-Reference](#)], the specification in this section applies also to combinations of RIF documents with OWL 1 ontologies.

OWL 2 specifies two different variants of the language, each having its own semantics, namely OWL 2 DL [[OWL2-Syntax](#)] (called simply OWL 2 in the specification) and OWL 2 Full [[OWL2-RDF-Based-Semantics](#)]. [OWL 1 Lite](#) and [OWL 1 DL](#) [[OWL-Reference](#)], which are sublanguages of OWL 1, can be seen as syntactical subsets of OWL 2 DL. The key difference between OWL 2 DL and OWL 2 Full is that the semantics of OWL 2 DL [[OWL2-Semantics](#)] is based on standard Description Logic semantics, whereas the semantics of OWL 2 Full is an extension of the RDFS semantics.

The syntax of OWL 2 is defined in terms of a structural specification, and there is a mapping to an RDF representation for interchange. The RDF representation of OWL 2 DL does not extend the RDF syntax, but rather restricts it: every OWL 2 DL ontology in RDF form is an RDF graph, but not every RDF graph is an OWL 2 DL

ontology. OWL 2 Full and RDF have the same syntax: every RDF graph is an OWL 2 Full ontology and vice versa. This syntactical difference is reflected in the definition of RIF-OWL compatibility: combinations of RIF with OWL 2 DL are based on the OWL 2 structural model, whereas combinations with OWL 2 Full are based on the RDF syntax.

Since the OWL 2 Full syntax is the same as the RDF syntax and the OWL 2 Full semantics is an extension of the RDF semantics, the definition of RIF-OWL 2 Full compatibility is an extension of RIF-RDF compatibility. However, defining RIF-OWL DL compatibility in the same way would entail losing certain semantic properties of OWL 2 DL. One of the main reasons for this is the difference in the way classes and properties are interpreted in OWL 2 Full and OWL 2 DL. In the Full variant, classes and properties are interpreted as objects in the domain of interpretation, which are then associated with subsets of, respectively binary relations over the domain of interpretation, using the `rdf:type` property and the extension function IEXT, as in RDF. In the DL variant, classes and properties are directly interpreted as subsets of, respectively binary relations over the domain. This is a key property of the first-order logic nature of Description Logic semantics and enables the use of Description Logic reasoning techniques for processing OWL 2 DL descriptions. Defining RIF-OWL DL compatibility as an extension of RIF-RDF compatibility would define a correspondence between OWL 2 DL statements and RIF frame formulas. Since RIF frame formulas are interpreted using an extension function, as in RDF, defining the correspondence between them and OWL 2 DL statements would change the semantics of OWL statements, even if the RIF document were empty.

A RIF-OWL combination that is faithful to the first-order nature of the OWL 2 DL semantics requires interpreting classes and properties as sets and binary relations, respectively, suggesting that a correspondence could be defined with unary and binary predicates. It is, however, also desirable that there be uniform syntax for the RIF component of both RIF-OWL 2 DL and RIF-RDF/OWL 2 Full combinations, because one may not know at the time of constructing the rules which type of inference will be used. Consider, for example, an RDF graph *S* consisting of the following statements

```
_ :x rdf:type owl:Ontology .
a  rdf:type C .
```

and a RIF document with the rule

```
forall ?x (?x[rdf:type -> D] :- ?x[rdf:type -> C])
```

The combination of the two, according to the specification of [RDF Compatibility](#), allows deriving the triple

```
a  rdf:type D .
```

Now, the RDF graph  $S$  is also an OWL 2 DL ontology. Therefore, one would expect the triple to be implied according to the semantics of RIF-OWL DL combinations as well.

To ensure that the RIF-OWL DL combination is faithful to the OWL 2 DL semantics and to enable using the same, or similar, RIF rules in combinations with both OWL 2 DL and RDF/OWL 2 Full, the interpretation of frame formulas  $s[p \rightarrow o]$  in RIF-OWL DL combinations is slightly different from their interpretation in RIF and syntactical restrictions are imposed on the use of variables and function terms in frame formulas.

The remainder of this section formally defines combinations of RIF rules with OWL 2 DL and OWL 2 Full ontologies and the semantics of such combinations. A combination consists of a RIF document and a set of OWL ontologies. The semantics of combinations is defined in terms of combined models, which are pairs of RIF semantic multi-structures and OWL 2 DL, respectively OWL 2 Full interpretations. The interaction between the structures and interpretations is defined through a number of conditions. Entailment is defined as model inclusion, as usual.

#### 4.1 Syntax of RIF-OWL Combinations

Since RDF graphs and OWL 2 Full ontologies cannot be distinguished, the syntax of RIF-OWL 2 Full combinations is the same as the syntax of [RIF-RDF combinations](#).

The syntax of [OWL ontologies](#) in RIF-OWL DL combinations is given by the structural specification of OWL 2 and the restrictions on OWL 2 DL ontologies [OWL2-Syntax](#). Certain restrictions are imposed on the syntax of the RIF rules in combinations with OWL 2 DL. Specifically, the only terms allowed in class and property positions in frame formulas are constant symbols. A DL-frame formula is a frame formula  $a[b_1 \rightarrow c_1 \dots b_n \rightarrow c_n]$  such that  $n \geq 1$  and for every  $b_i$ , with  $1 \leq i \leq n$ , it holds that  $b_i$  is a constant symbol and if  $b_i = \text{rdf:type}$ , then  $c_i$  is a constant symbol.

**Definition.** A [condition formula](#)  $\phi$  is a **DL-condition** if every frame formula in  $\phi$  is a DL-frame formula.

A [RIF-BLD document formula](#)  $R$  is a **RIF-BLD DL-document formula** if every frame formula in  $R$  is a DL-frame formula.

A **RIF-OWL DL-combination** is a pair  $\langle R, \mathbf{O} \rangle$ , where  $R$  is a [RIF-BLD DL-document formula](#) and  $\mathbf{O}$  is a set of [OWL 2 DL ontologies](#) of a [vocabulary](#)  $V$  over an [OWL 2 datatype map](#)  $D$ .  $\square$

When clear from the context, RIF-OWL DL-combinations are referred to simply as *combinations*.

#### 4.1.1 Safeness Restrictions

In the literature, several restrictions on the use of variables in combinations of rules and Description Logics have been identified [Motik05, Rosati06] for the purpose of decidable reasoning. This section specifies such safeness restrictions for RIF-OWL2-DL combinations.

Given a set of OWL 2 DL ontologies  $\mathbf{O}$ , a variable  $?x$  in a RIF rule  $\mathbf{Q} \ H :- B$  is **DL-safe** if it occurs in an atomic formula in  $B$  that is not of the form  $s[P \rightarrow o]$  or  $s[\text{rdf:type} \rightarrow A]$ , where  $s$ ,  $P$ ,  $o$ , and  $A$  are terms (possibly including  $?x$ ) and  $P$  or  $A$  occurs in one of the ontologies in  $\mathbf{O}$ . A disjunction-free RIF rule  $\mathbf{Q} \ (H :- B)$  is **DL-safe**, given  $\mathbf{O}$ , if every variable that occurs in  $H :- B$  is DL-safe. A disjunction-free RIF rule  $\mathbf{Q} \ (H :- B)$  is **weakly DL-safe**, given  $\mathbf{O}$ , if every variable that occurs in  $H$  is DL-safe.

**Definition.** A [RIF-OWL DL-combination](#)  $\langle R, \mathbf{O} \rangle$  is **DL-safe** if every rule in  $R$  is DL-safe, given  $\mathbf{O}$ . A [RIF-OWL DL-combination](#)  $\langle R, \mathbf{O} \rangle$  is **weakly DL-safe** if every rule in  $R$  is weakly DL-safe, given  $\mathbf{O}$ .  $\square$

#### Feature At Risk #2: Safeness

*Note: This feature is "at risk" and may be removed from this specification based on feedback. Please send feedback to [public-rif-comments@w3.org](mailto:public-rif-comments@w3.org).*

The above definition of DL-safeness is intended to identify a fragment of RIF-OWL DL combinations for which reasoning is decidable. This definition should be considered **AT RISK** and may become stricter based on implementation experience.

#### 4.1.2 Datatypes in OWL 2

Compared with RDF and the RIF, OWL 2 uses a slightly extended notion of datatype.

In the remainder of this section, a datatype  $d$  contains, in addition to the lexical space, value space, and lexical-to-value mapping, a **facet space**, which is a set of pairs of the form  $(F, v)$ , where  $F$  is an IRI and  $v$  is a data value, and a **facet-to-value mapping**, which is a mapping from facets to subsets of the value space of  $d$ .

An **OWL 2 datatype map**  $D$  is a datatype map that maps the IRIs of the datatypes specified in [Section 4](#) of [OWL2-Syntax] to the corresponding datatypes such that the domain of  $D$  does not include `rdfs:Literal`.

We note here that the [definitions of datatype and datatype map in the OWL 2 direct semantics](#) specification [[OWL2-Semantics](#)] are somewhat different. There, a datatype is some entity with some associated IRIs, and the datatype map assigns lexical value, and facet spaces, as well as lexical-to-value and facet-to-value mappings. The definitions of datatype and datatype map we use are isomorphic, and, indeed, the same as in the [OWL 2 RDF-based semantics](#) specification [[OWL2-RDF-Based-Semantics](#)]. The latter does not preclude the use of `rdfs:Literal` in datatype maps. Note that we do not restrict the use of `rdfs:Literal` in OWL 2 ontologies or RDF graphs.

## 4.2 Semantics of RIF-OWL Combinations

The semantics of RIF-OWL 2 Full combinations is a straightforward extension of the [Semantics of RIF-RDF Combinations](#).

The semantics of RIF-OWL2 DL combinations cannot straightforwardly extend the semantics of RIF-RDF combinations, because OWL 2 DL does not extend the RDF semantics. In order to keep the syntax of the rules uniform between RIF-OWL 2 Full and RIF-OWL DL combinations, the semantics of RIF frame formulas is slightly altered in RIF-OWL DL combinations.

### 4.2.1 OWL Full

Given an [OWL 2 datatype map  \$D\$](#)  and a vocabulary  $V$  that includes the domain of  $D$  and the OWL 2 Full [vocabulary](#) and [facet names](#), a [D-interpretation  \$I\$](#)  is an **OWL 2 RDF-Based Interpretation** of  $V$  with respect to  $D$  if it satisfies the semantic conditions in [Section 5](#) of [[OWL2-RDF-Based-Semantics](#)].

The semantics of RIF-OWL 2 Full combinations is a straightforward extension of the semantics of RIF-RDF combinations. It is based on the same notion of [common interpretations](#), but defines additional notions of satisfiability and entailment.

**Definition.** Let  $(\hat{I}, I)$  be a [common-RIF-RDF-interpretation](#) that is a [model](#) of a [RIF-RDF combination](#)  $C = \langle R, S \rangle$  and let  $D$  be an [OWL 2 datatype map conforming](#) with the set of datatypes in  $I$ .  $(\hat{I}, I)$  is an **RIF-OWL Full-model** of  $C$  if  $I$  is an [OWL 2 RDF-Based Interpretation](#) with respect to  $D$ ; in this case  $C$  is **RIF-OWL Full-satisfiable** with respect to  $D$ .

Let  $C$  be a RIF-RDF combination, let  $S$  be a [generalized RDF graph](#), let  $\varphi$  be a [condition formula](#), and let  $D$  be an [OWL 2 datatype map  \$D\$  conforming](#) with the set of [considered datatypes](#).  $C$  **RIF-OWL Full-entails**  $S$  with respect to  $D$  if every [RIF-OWL Full-model](#) of  $C$  [satisfies](#)  $S$ . Likewise,  $C$  **RIF-OWL Full-entails**  $\varphi$  with respect to  $D$  if every [RIF-OWL Full-model](#) of  $C$  [satisfies](#)  $\varphi$ .  $\square$

#### 4.2.2 OWL DL

The semantics of RIF-OWL DL-combinations is similar in spirit to the semantics of RIF-RDF combinations. Analogous to common-RIF-RDF-interpretations, there is the notion of common-RIF-OWL DL-interpretations, which are pairs of RIF and OWL 2 DL interpretations, and which define a number of conditions that relate these interpretations to each other.

##### 4.2.2.1 Modified Semantics for RIF Frame Formulas

The modification of the semantics of RIF frame formulas is achieved by modifying the mapping function for frame formulas ( $I_{\text{frame}}$ ), and leaving the RIF BLD semantics [RIF-BLD] otherwise unchanged.

Namely, frame formulas of the form  $s[\text{rdf:type} \rightarrow o]$  are interpreted as membership of  $s$  in the set denoted by  $o$  and frame formulas of the form  $s[p \rightarrow o]$ , where  $p$  is not  $\text{rdf:type}$ , as membership of the pair  $(s, o)$  in the binary relation denoted by  $p$ .

**Definition.** A **dl-semantic structure** is a tuple  $I = \langle TV, DTS, D, D_{\text{ind}}, D_{\text{func}}, I_C, I_V, I_F, I_{\text{frame}}, I_{\text{NF}}, I_{\text{sub}}, I_{\text{isa}}, I_{\text{=}}, I_{\text{external}}, I_{\text{truth}} \rangle$ , where

- $I_C$  is defined like in [RIF semantic structures](#), with the difference that for constants appearing as attribute  $b_i$  or value  $c_i$  in any frame formula  $a[b_1 \rightarrow c_1 \dots b_n \rightarrow c_n]$  it is not required that  $I_C(b_i) \in D_{\text{ind}}$  or  $I_C(c_i) \in D_{\text{ind}}$  and ;
- $I_{\text{frame}}$  is a mapping from  $D_{\text{ind}}$  to total functions of the form  $\text{SetOfFiniteBags}(D \times D) \rightarrow D$  such that for each pair  $(u, v) \in \text{SetOfFiniteBags}(D \setminus D_{\text{ind}} \times D)$  it holds that  $u \neq I_C(\text{rdf:type})$  if and only if  $v \in D_{\text{ind}}$ ;
- all other elements of the structure are defined as in [RIF semantic structures](#).

DL-semantic multi-structures are defined analogous to [RIF-BLD semantic multi-structures](#) [RIF-BLD]. Formally, a **dl-semantic multi-structure**  $\hat{I}$  is a set of dl-semantic structures  $\{J, I, I^{i_1}, I^{i_2}, \dots\}$ , where

- $I$  and  $J$  are dl-semantic structures; and
- $I^{i_1}, I^{i_2}$ , etc., are dl-semantic structures **adorned** with the [locators](#) of *distinct* RIF-BLD formulas (one can think of these adorned structures as locator-structure pairs).

All the structures in  $\hat{I}$  (adorned and non-adorned) are identical in all respects except for the following:

- The mappings  $J_C$ ,  $I_C$ ,  $I_C^{i1}$ ,  $I_C^{i2}$ , ... may differ on the constants in `Const` that belong to the [rif:local](#) symbol space.
- The mappings  $J_V$ ,  $I_V$ ,  $I_V^{i1}$ ,  $I_V^{i2}$  may differ.

The notation  $I(\varphi)$ , for any other formula or symbol  $\varphi$ , and the truth valuation function  $TVaI$  are defined as in [BLD semantic structures](#).

**Definition.** A [dl-semantic multi-structure](#)  $\hat{I}$  is a *model* of a [RIF-BLD DL-document formula](#)  $R$  if  $TVaI(R)=t$ .  $\square$

#### 4.2.2.2 Semantics of RIF-OWL DL Combinations

As defined in [\[OWL2-Semantics\]](#), an [interpretation](#) for a vocabulary  $V$  over a datatype map  $D$  is a tuple  $I = \langle IR, LV, C, OP, DP, I, DT, LT, FA \rangle$ , where

- $IR$  is a non-empty set, called the object domain,
- $LV$  is a non-empty set, called the data domain, which includes all value spaces of the datatypes in the range of  $D$ ,
- $C$  is a mapping from classes to subsets of  $IR$ ,
- $OP$  is a mapping from object properties to subsets of  $IR \times IR$ ,
- $DP$  is a mapping from object properties to subsets of  $IR \times LV$ ,
- $I$  is a mapping from individuals into  $IR$ ,
- $DT$  is a mapping from datatypes to subsets of  $LV$ ,
- $LT$  is a mapping from typed literals in  $V$  into  $LV$ , and
- $FA$  is a mapping from IRI, literal pairs to subsets of value spaces in  $D$ .

The OWL semantics imposes a number of [further restrictions](#) on the mapping functions to ensure the interpretation of datatypes, literals, and facets conforms with the given datatype map  $D$  and to define the semantics of built-in classes and properties (e.g., `owl:Thing`). The mappings  $DT$ ,  $LT$ , and  $FA$  are essentially given by the datatype map.

**Definition.** Given a vocabulary  $V$  over an [OWL 2 datatype map](#)  $D$ , a *common-RIF-OWL DL-interpretation* for  $V$  over  $D$  is a pair  $(\hat{I}, I)$ , where  $\hat{I}$  is a [dl-semantic multi-structure](#) of the form  $\{J, I, I^{i1}, I^{i2}, \dots\}$ , and  $I$  is an [interpretation](#) for  $V$  over  $D$ , such that the following conditions hold.

1.  $D$  is conforming with the datatypes in  $I$ ;
2.  $(IR \cup LV)$  is *Dind*;
3.  $C(c)$  is the set of all objects  $k$  such that  $I_{\text{truth}}(I_{\text{frame}}(k)(\{I_C(\text{rdf:type}), I_C(\langle c \rangle)\})) = t$ , for every IRI  $c$  in  $V$ ;
4.  $OP(p)$  is the set of all pairs  $(k, l)$  such that  $I_{\text{truth}}(I_{\text{frame}}(k)(\{I_C(\langle p \rangle), l\})) = t$  (true), for every IRI  $p$  identifying an object property in  $V$ ;
5.  $DP(p)$  is the set of all pairs  $(k, l)$  such that  $I_{\text{truth}}(I_{\text{frame}}(k)(\{I_C(\langle p \rangle), l\})) = t$  (true), for every IRI  $p$  identifying a data property in  $V$ ;
6.  $I(i) = I_C(\langle i \rangle)$  for every IRI  $i$  identifying an individual in  $V$ .  $\square$

Condition 2 ensures that the relevant parts of the domains of interpretation are the same. Condition 3 ensures that the interpretation (extension) of an OWL class identified by an IRI  $u$  corresponds to the interpretation of frames of the form  $?x[\text{rdf:type} \rightarrow \langle u \rangle]$ . Conditions 4 and 5 ensure that the interpretation (extension) of an OWL object or data property identified by an IRI  $u$  corresponds to the interpretation of frames of the form  $?x[\langle u \rangle \rightarrow ?y]$ . Finally, condition 6 ensures that individual identifiers in the OWL ontologies and the RIF documents are interpreted in the same way.

Using the definition of common-RIF-OWL DL-interpretation, satisfaction, models, and entailment are defined in the usual way:

**Definition.** A [common-RIF-OWL DL-interpretation](#)  $(\hat{I}, I)$  for a vocabulary  $V$  over an [OWL 2 datatype map](#)  $D$  is an *RIF-OWL DL-model* of a [RIF-OWL DL-combination](#)  $C = \langle R, O \rangle$  if  $\hat{I}$  is a [model](#) of  $R$  and  $I$  is a [model](#) of every ontology  $O$  in  $O$ ; in this case  $C$  is *RIF-OWL DL-satisfiable* for  $V$  over  $D$ .  $(\hat{I}, I)$  is an *RIF-OWL DL-model* of an OWL 2 ontology  $O$  if  $I$  is a [model](#) of  $O$ .  $(\hat{I}, I)$  is an *RIF-OWL DL-model* of a [DL-condition formula](#)  $\varphi$  if  $TVaI(\varphi) = t$ .

Let  $C$  be a RIF-OWL DL-combination, let  $O$  be an OWL 2 ontology, let  $\varphi$  be a [DL-condition formula](#), and let  $D$  be an [OWL 2 datatype map conforming](#) with the set of [considered datatypes](#), and let  $V$  be a vocabulary over  $D$  for every ontology in  $C$  and for  $O$ .  $C$  *RIF-OWL DL-entails*  $O$  with respect to  $D$  if every common-RIF-OWL DL-interpretation for  $V$  over  $D$  that is an [RIF-OWL DL-model](#) of  $C$  is an [RIF-OWL DL-model](#) of  $O$ . Likewise,  $C$  *RIF-OWL DL-entails*  $\varphi$  with respect to  $D$  if every common-RIF-OWL DL-interpretation for  $V$  over  $D$  that is an [RIF-OWL DL-model](#) of  $C$  is an [RIF-OWL DL-model](#) of  $\varphi$ .  $\square$

**Example.** In OWL 2 DL, the domains for interpreting individuals respectively, literals (data values), are disjoint. The disjointness entails that data values cannot be members of a class and individuals cannot be members of a datatype.

RIF does not make such distinctions; variable quantification ranges over the entire domain. So, the same variable may be assigned to an abstract individual or a concrete data value. Additionally, RIF constants (e.g., IRIs) denoting individuals can be written in place of a data value, such as the value of a data-valued property or in datatype membership statements; similarly for constants denoting data values. Such statements cannot be satisfied in any common-RIF-OWL DL-interpretation. The following example illustrates several such statements.

Consider the datatype `xs:string` and a RIF-OWL DL combination consisting of the set containing only the OWL DL ontology

```
ex:myiri rdf:type ex:A .
```

and a RIF document containing the following fact

```
ex:myiri[rdf:type -> xs:string]
```

This combination is not [RIF-OWL DL-satisfiable](#), because `ex:myiri` is an individual identifier and `S` maps individual identifiers to elements in `O`, which is disjoint from the elements in the datatype `xs:string`.

Consider a RIF-OWL DL combination consisting of the set containing only the OWL 2 DL ontology

```
ex:hasChild rdf:type owl:ObjectProperty .
```

and a RIF document containing the following fact

```
ex:myiri[ex:hasChild -> "John"]
```

This combination is not [RIF-OWL DL-satisfiable](#), because `ex:hasChild` is an object property, and values of object properties may not be concrete data values.

Consider a RIF-OWL DL combination consisting of the OWL DL ontology

```
SubClassof(ex:A ex:B)
```

and a RIF document containing the following rule

```
forall ?x (?x[rdf:type -> ex:A])
```

This combination is not [RIF-OWL DL-satisfiable](#), because the rule requires every element, including every concrete data value, to be a member of the class `ex:A`. However, since every OWL interpretation requires every member of `ex:A` to be an element of the object domain, concrete data values cannot be members of the object domain.  $\square$

## 5 Importing RDF and OWL in RIF

In the preceding sections, [RIF-RDF Combinations](#) and [RIF-OWL combinations](#) were defined in an abstract way, as pairs consisting of a RIF document and a set of RDF graphs/OWL ontologies. In addition, different semantics were specified based on the various RDF and OWL entailment regimes. RIF provides a mechanism for explicitly referring to (importing) RDF graphs from documents and specifying the intended profile (entailment regime) through the use of `Import` statements.

This section specifies how RIF documents with such import statements must be interpreted.

A [RIF document](#) contains a number of `Import` statements. Unary `Import` statements are used for importing RIF documents, and the interpretation of these

statements is defined in [Section 3.5](#) of [RIF-BLD]. This section defines the interpretation of binary `Import` statements:

```
Import(<t1> <p1>
  ...
Import(<tn> <pn>)
```

Here,  $t_i$  is an absolute IRI referring to an RDF graph to be imported and  $p_i$  is an absolute IRI denoting the profile to be used for the import.

The profile determines which notions of model, satisfiability and entailment must be used. For example, if a RIF document  $R$  imports an RDF graph  $S$  with the profile *RDFS*, the notions of [RIF-RDFS-model](#), [RIF-RDFS-satisfiability](#), and [RIF-RDFS-entailment](#) must be used for the combination  $\langle R, \{S\} \rangle$ .

Profiles are ordered as specified in [Section 5.1.1](#). If several graphs are imported in a document, and these imports specify different profiles, the highest of these profiles is used. For example, if a RIF document  $R$  imports an RDF graph  $S_1$  with the profile *RDF* and an RDF graph  $S_2$  with the profile *OWL Full*, the notions of [RIF-OWL Full-model](#), [RIF-OWL Full-satisfiability](#), and [RIF-OWL Full-entailment](#) must be used with the combination  $\langle R, \{S_1, S_2\} \rangle$ .

Finally, if a [RIF document](#)  $R$  imports an RDF graph  $S$  with the profile *OWL DL*,  $R$  must be a [RIF-BLD DL-document formula](#),  $S$  must be the [RDF representation](#) of an OWL 2 ontology  $O$ , and the notions of [RIF-OWL DL-model](#), [RIF-OWL DL-satisfiability](#), and [RIF-OWL DL-entailment](#) must be used with the combination  $\langle R, \{O\} \rangle$ .

## 5.1 Profiles of Imports

RIF defines specific profiles for the different notions of model, satisfiability and entailment of combinations, as well as one generic profile. The use of a specific profile specifies how a combination should be interpreted. If a specific profile cannot be handled by a receiver, the combination should be rejected. The use of a generic profile implies that a receiver may interpret the combination to the best of its ability.

The use of profiles is not restricted to the profiles specified in this document. Any specific profile that is used with RIF must specify an IRI that identifies it, as well as associated notions of model, satisfiability, and entailment for combinations.

### 5.1.1 Specific Profiles

The following table lists the specific profiles defined by RIF, the IRIs of these profiles, and the notions of model, satisfiability, and entailment that must be used with the profile.

Specific profiles in RIF.

Profile	IRI of the Profile	Model	Satisfiability	Entailment
Simple	<a href="http://www.w3.org/2007/rif-import-profile#Simple">http://www.w3.org/2007/rif-import-profile#Simple</a>	<a href="#">RIF-Simple-model</a>	<a href="#">satisfiability</a>	<a href="#">RIF-Simple-entailment</a>
RDF	<a href="http://www.w3.org/2007/rif-import-profile#RDF">http://www.w3.org/2007/rif-import-profile#RDF</a>	<a href="#">RIF-RDF-model</a>	<a href="#">RIF-RDF-satisfiability</a>	<a href="#">RIF-RDF-entailment</a>
RDFS	<a href="http://www.w3.org/2007/rif-import-profile#RDFS">http://www.w3.org/2007/rif-import-profile#RDFS</a>	<a href="#">RIF-RDFS-model</a>	<a href="#">RIF-RDFS-satisfiability</a>	<a href="#">RIF-RDFS-entailment</a>
D	<a href="http://www.w3.org/2007/rif-import-profile#D">http://www.w3.org/2007/rif-import-profile#D</a>	<a href="#">RIF-D-model</a>	<a href="#">RIF-D-satisfiability</a>	<a href="#">RIF-D-entailment</a>
OWL DL	<a href="http://www.w3.org/2007/rif-import-profile#OWL-DL">http://www.w3.org/2007/rif-import-profile#OWL-DL</a>	<a href="#">RIF-OWL-DL-model</a>	<a href="#">RIF-OWL-DL-satisfiability</a>	<a href="#">RIF-OWL-DL-entailment</a>
OWL Full	<a href="http://www.w3.org/2007/rif-import-profile#OWL-Full">http://www.w3.org/2007/rif-import-profile#OWL-Full</a>	<a href="#">RIF-OWL-Full-model</a>	<a href="#">RIF-OWL-Full-satisfiability</a>	<a href="#">RIF-OWL-Full-entailment</a>

Profiles that are defined for combinations of DL-document formulas and OWL ontologies in abstract syntax form are called *DL profiles*. Of the mentioned profiles, the profile *OWL DL* is a DL profile.

The profiles are ordered as follows, where '<' reads "is lower than":

Simple < RDF < RDFS < D < OWL Full

OWL DL < OWL Full

### 5.1.2 Generic Profile

RIF specifies one generic profile. The use of the generic profile does not imply the use of a specific notion of model, satisfiability, and entailment.

Generic profile in RIF.

Profile	IRI of the Profile
Generic	< <a href="http://www.w3.org/2007/rif-import-profile#Generic">http://www.w3.org/2007/rif-import-profile#Generic</a> >

## 5.2 Interpretation of Profiles

Let  $R$  be a [RIF document](#) such that

```
Import (<u1> <p1>)
...
Import (<un> <pn>)
```

are all the two-ary import statements in  $R$  and the documents [imported](#) into  $R$  and let  $Profile$  be the set of profiles corresponding to the IRIs  $p_1, \dots, p_n$ .

If  $p_i, 1 \leq i \leq n$ , corresponds to a DL profile and  $u_i$  refers to an RDF graph that is not the RDF representation of an OWL (2) DL ontology, the document should be rejected.

If  $u_i, 1 \leq i \leq n$ , refers to an RDF graph that uses a typed literal of the form `"s"^^rif:iri` or `"s"^^rdf:PlainLiteral`, the document must be rejected.

If  $Profile$  contains only specific profiles, then:

- If  $Profile$  does not have a single highest profile, the document must be rejected.
- If  $Profile$  contains only DL profiles and  $R$  is not a DL-document formula, it must be rejected.
- If  $Profile$  contains only DL profiles and the RDF graphs referred to by  $u_1, \dots, u_n$  are RDF representations of the OWL 2 ontologies  $O_1, \dots, O_n$ , then the combination  $C = \langle R, \{O_1, \dots, O_n\} \rangle$  must be interpreted according to the highest among the profiles in  $Profile$ .
- Otherwise, the combination  $C = \langle R, \{S_1, \dots, S_n\} \rangle$ , where  $S_1, \dots, S_n$  are the RDF graphs referred to by  $u_1, \dots, u_n$ , must be interpreted according to the highest among the profiles in  $Profile$ .

If  $Profile$  contains a generic profile, then the combination  $C = \langle R, \{S_1, \dots, S_n\} \rangle$ , where  $S_1, \dots, S_n$  are the RDF graphs referred to by  $u_1, \dots, u_n$ , may be interpreted according to the highest among the specific profiles in  $Profile$ , if there is one.

## 6 Conformance Clauses

We define notions of conformance for RIF-RDF and RIF-OWL combinations. We define these notions both for the RIF Core [[RIF-Core](#)] and RIF BLD [[RIF-BLD](#)] dialects.

Conformance is described in terms of semantics-preserving transformations between the native syntax of a compliant processor and the XML syntax of RIF Core and BLD.

We say that an RDF graph  $S$  is a *standard RDF graph* if for every triple  $s \ p \ o$  in  $S$ ,  $s$  is an IRI or blank node,  $p$  is an IRI, and  $o$  is an IRI, literal, or blank node. A combination  $\langle R, \mathbf{S} \rangle$  is *standard* if every graph in  $\mathbf{S}$  is standard.

Each RIF processor has sets  $T$ , of supported datatypes and symbol spaces that include the [symbol spaces](#) listed in [RIF-DTB], and  $E$ , of supported external terms that include the built-ins listed in [RIF-DTB]. The datatype map of a RIF processor is the smallest datatype map conforming with the set of datatypes in  $T$ .

Now, let  $P \in \{\text{Simple, RDF, RDFS, D, OWL Full}\}$  be a [specific RDF profile](#). A [RIF-RDF combination](#)  $C = \langle R, \mathbf{S} \rangle$  is a  $BLD_{T,E-P}$  combination if  $R$  is a  $BLD_{T,E}$  formula and  $C$  is a  $Core_{T,E-P}$  combination if  $R$  is a  $Core_{T,E}$  formula.

A [RIF-OWL DL-combination](#)  $C = \langle R, \mathbf{O} \rangle$  is a  $BLD_{T,E-OWL}$  DL combination if  $R$  is a  $BLD_{T,E}$  formula and  $C$  is a  $Core_{T,E-OWL}$  DL combination if  $R$  is a  $Core_{T,E}$  formula.

A RIF processor is a **conformant  $BLD_{T,E-P}$  consumer**, for  $P \in \{\text{Simple, RDF, RDFS, D, OWL DL, OWL Full}\}$ , iff it implements a *semantics-preserving mapping*,  $\mu$ , from the set of standard  $BLD_{T,E-P}$  combinations, standard RDF graphs, OWL 2 ontologies, and  $BLD_{T,E}$  formulas to the language  $L$  of the processor ( $\mu$  does not need to be an "onto" mapping) and, in case  $P \in \{\text{OWL DL, OWL Full}\}$ , its datatype map is an [OWL 2 datatype map](#).

We say that a RIF document  $R$  is list-safe if  $R$  is [safe](#) and it contains no occurrences of `rdf:first`, `rdf:rest`, or `rdf:nil` in rule consequents. An RDF graph  $S$  is list-safe if it contains no occurrences of `rdf:first` or `rdf:rest` outside of the property positions, it contains no occurrences of `rdf:nil` outside of triples of the form `... rdf:rest rdf:nil`, and there are no two triples `s rdf:first o1 . s rdf:first o2 .` or `s rdf:rest o1 . s rdf:rest o2 .` in  $S$ , where  $s$ ,  $o1$ ,  $o2$  are RDF terms and  $o1 \neq o2$ . A combination  $\langle R, \mathbf{S} \rangle$  is **list-safe** if  $R$  is list-safe and the [merge](#) of the graphs in  $\mathbf{S}$  is list-safe.

A RIF processor is a **conformant  $Core_{T,E-P}$  consumer**, for  $P \in \{\text{Simple, RDF, RDFS, D, OWL DL, OWL Full}\}$ , iff it implements a *semantics-preserving mapping*,  $\mu$ , from the set of standard list-safe  $Core_{T,E-P}$  combinations, standard RDF graphs, OWL 2 ontologies, and  $Core_{T,E}$  formulas to the language  $L$  of the processor ( $\mu$  does not need to be an "onto" mapping) and, in case  $P \in \{\text{OWL DL, OWL Full}\}$ , its datatype map is an [OWL 2 datatype map](#).

Formally, this means that for any pair  $(\varphi, \psi)$ , where  $\varphi$  is a  $BLD_{T,E-P}$  combination and  $\psi$  is an RDF graph, OWL 2 ontology, or  $BLD_{T,E}$  formula such that  $\varphi \models_P \psi$  is defined,  $\varphi \models_P \psi$  iff  $\mu(\varphi) \models_L \mu(\psi)$ . Here  $\models_P$  denotes  $P$ -entailment and  $\models_L$  denotes the logical entailment in the language  $L$  of the RIF processor.

A RIF processor is a **conformant  $BLD_{T,E-P}$  producer** iff it implements a *semantics-preserving mapping*,  $\nu$ , from the language  $L$  of the processor to the set

of all  $BLD_{T,E}$  formulas, RDF graphs, OWL 2 ontologies, and  $BLD_{T,E-P}$  combinations ( $v$  does not need to be an "onto" mapping).

A RIF processor is a **conformant**  $Core_{T,E-P}$  **producer** iff it implements a *semantics-preserving mapping*,  $v$ , from the language  $L$  of the processor to the set of all  $Core_{T,E}$  formulas, RDF graphs, OWL 2 ontologies, and  $Core_{T,E-P}$  combinations ( $v$  does not need to be an "onto" mapping).

Formally, this means that for any pair  $(\phi, \psi)$  of formulas in  $L$  such that  $\phi \models_L \psi$  is defined,  $\phi \models_L \psi$  iff  $v(\phi) \models_P v(\psi)$ . Here  $\models_P$  denotes  $P$ -entailment and  $\models_L$  denotes the logical entailment in the language  $L$  of the RIF processor.

## 7 Acknowledgements

This document is the product of the Rules Interchange Format (RIF) Working Group (see below), the members of which deserve recognition for their time and commitment to RIF. The editors extend special thanks to: Mike Dean, Michael Kifer, Stella Mitchell, Axel Polleres, and Dave Reynolds, for their thorough reviews and insightful discussions; the working group chairs, Chris Welty and Christian de Sainte-Marie, for their invaluable technical help and inspirational leadership; and W3C staff contact Sandro Hawke, a constant source of ideas, help, and feedback.

The following members of the joint RIF-OWL task force have contributed to the [OWL Compatibility](#) section in this document: Mike Dean, Peter F. Patel-Schneider, and Ulrike Sattler.

The regular attendees at meetings of the Rule Interchange Format (RIF) Working Group at the time of the publication were: Adrian Paschke (Freie Universitaet Berlin), Axel Polleres (DERI), Changhai Ke (ILOG), Chris Welty (IBM), Christian de Sainte Marie (ILOG), Dave Reynolds (HP), Gary Hallmark (ORACLE), Harold Boley (NRC), Hassan Ait-Kaci (ILOG), Jos de Bruijn (FUB), Leora Morgenstern (IBM), Michael Kifer (Stony Brook), Mike Dean (BBN), Sandro Hawke (W3C/MIT), and Stella Mitchell (IBM).

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## 9 Appendix: Embeddings (Informative)

RIF-RDF combinations can be embedded into RIF documents in a fairly straightforward way, thereby demonstrating how a RIF-compliant translator without native support for RDF can process RIF-RDF combinations. RIF-OWL combinations cannot be embedded in RIF, in the general case. However, there is a subset of OWL 2 DL, namely the OWL 2 RL profile [[OWL2-Profiles](#)], for which RIF-OWL combinations that can be embedded.

Simple, RDF, and RDFS entailment for RIF-RDF combinations are embedded in RIF Core. RIF-OWL 2 RL combinations require reasoning with equality, and thus could not be embedded in RIF Core; they are embedded in RIF BLD.

The embeddings are defined using an embedding function  $tr$  that maps symbols, triples, and RDF graphs/OWL ontologies to RIF symbols, statements, and documents, respectively.

To embed consistency checking in RDF(S) and OWL, we use a special 0-ary predicate symbol `rif:error`, which is assumed not to be used in the RIF documents in the combination.

Besides the namespace prefixes defined in the [Overview](#), the following namespace prefix is used in this appendix: `pred` refers to the RIF namespace for built-in predicates <http://www.w3.org/2007/rif-builtin-predicate#> [[RIF-DTB](#)].

To facilitate the definition of the embeddings we define the notion of a *merge* of RIF formulas.

**Definition.** Let  $\mathbf{R}=\{R_1,\dots,R_n\}$  be a set of [document, group, and rule formulas](#), such that there are no prefix or base directives, or relative IRIs in  $\mathbf{R}$  and  $directive_{i1}, \dots, directive_{nm}$  are all the [import directives](#) occurring in document formulas in  $\mathbf{R}$ . The *merge* of  $\mathbf{R}$ , denoted  $merge(\mathbf{R})$ , is defined as  $Document(directive_{i1} \dots directive_{nm} Group(R^*_1 \dots R^*_n))$ , where  $R^*_i$  is obtained from  $R_i$  in the following way:

- if  $R_i$  is a document formula of the form  $Document(directive_{i1} \dots directive_{im} \Gamma)$ , then  $R^*_i=\Gamma$  and
- if  $R_i$  is a non-document formula (i.e., fact, rule, or group), then  $R^*_i=R_i$ .  $\square$

Note that the requirement that no prefix or based directives, or relative IRIs are included in any of the formulas to be merged is not a limitation, since compact IRIs can be rewritten to absolute IRIs, as can relative IRIs, by exploiting prefix and base directives, and the location of the document.

## 9.1 Embedding RIF-RDF Combinations

RIF-RDF combinations are embedded by combining the RIF rules with embeddings of the RDF graphs and an axiomatization of Simple, RDF, and RDFS entailment.

The embedding is not defined for combinations that include infinite RDF graphs and for combinations that include RDF graphs with RDF URI references that are not absolute IRIs (see the [End note on RDF URI references](#)) or plain literals that are not in the lexical space of the `xs:string` datatype [XML-Schema2]. Also, the embedding is not defined for RDF lists.

We define a list-free combination as a combination that does not contain any mention of the symbols `rdf:first`, `rdf:rest`, or `rdf:nil`.

In the remainder of this section we first define the embedding of symbols, triples, and graphs, after which we define the axiomatization of Simple, RDF, and RDFS entailment of combinations and, finally, demonstrate faithfulness of the embeddings.

### 9.1.1 Embedding Symbols

Given a [combination](#)  $C = \langle R, S \rangle$ , the function `tr` maps RDF symbols of a vocabulary  $V$  and a set of blank nodes  $B$  to RIF symbols, as defined in the following table. It is assumed that the vocabulary  $V$  includes all the IRIs and literals used in the RIF documents and condition formulas under consideration.

In the table, the mapping `tr'` is an injective function that maps typed literals to new constants in the `rif:local` symbol space, where a new constant is a constant that is not used in the document or its vicinity (i.e., entailed formula or entailing combination). It "generates" a new constant from a typed literal.

Mapping RDF symbols to RIF.

RDF Symbol	RIF Symbol	Mapping
IRI $i$ in $V_U$	Constant with symbol space <code>rif:iri</code>	$\text{tr}(i) = \langle i \rangle$
Blank node $_ : x$ in $B$	Variable symbol <code>?x</code>	$\text{tr}(_ : x) = ?x$
Plain literal without a	Constant with the datatype <code>xs:string</code>	$\text{tr}(\text{"xxx"}) = \text{"xxx"}$

language tag xxx in <i>VPL</i>		
Plain literal with a language tag "xxx"@lang in <i>VPL</i>	Constant with the datatype rdf:PlainLiteral	$\text{tr}(\text{"xxx"@lang}) = \text{"xxx@lang"}^{\wedge}\text{rdf:PlainLiteral}$
Well-typed literal "s"^^u in <i>VTL</i>	Constant with the symbol space u	$\text{tr}(\text{"s"}^{\wedge}\text{u}) = \text{"s"}^{\wedge}\text{u}$
Non-well- typed literal "s"^^u in <i>VTL</i>	Local constant s-u' that is not used in C and is obtained from "s"^^u	$\text{tr}(\text{"s"}^{\wedge}\text{u}) = \text{tr}'(\text{"s"}^{\wedge}\text{u})$

### 9.1.2 Embedding Triples and Graphs

This section extends the mapping function  $\text{tr}$  to triples and defines two embedding functions for RDF graphs. In one embedding ( $\text{tr}_R$ ), graphs are embedded as RIF documents and variables (originating from blank nodes) are skolemized, i.e., replaced with new constant symbols. In the other embedding ( $\text{tr}_Q$ ), graphs are embedded as condition formulas and variables (originating from blank nodes) are existentially quantified. The following sections show how these embeddings can be used for reasoning with combinations.

For skolemization we assume a function  $\text{sk}$  that takes as argument a formula  $\phi$  and returns a formula  $\phi'$  that is obtained from  $\phi$  by replacing every variable symbol  $?x$  with  $\langle \text{new-iri} \rangle$ , where  $\text{new-iri}$  is a new globally unique IRI, i.e., it does not occur in the graph or its vicinity (i.e., entailing combination or entailed graph/formula).

RDF Construct	RIF Construct	Mapping
Triple s p o .	Frame formula $\text{tr}(s) [\text{tr}(p)$ $\rightarrow \text{tr}(o)]$	$\text{tr}(s \ p \ o \ .) = \text{tr}(s) [\text{tr}(p) \rightarrow \text{tr}(o)]$
Graph S	Group formula $\text{tr}_R(S)$	$\text{tr}_R(S) = \text{sk}(\text{Document } (\text{Group } (\text{tr}(t_1) \dots \text{tr}(t_m)) \ ))$ , where $t_1, \dots, t_m$ are the triples in S

Graph S	Condition formula $tr_Q(S)$	$tr_Q(S) = \text{Exists } tr(x_1) \dots tr(x_n) (\text{And}(tr(t_1) \dots tr(t_m)))$ , where $x_1, \dots, x_n$ are the blank nodes occurring in S and $t_1, \dots, t_m$ are the triples in S
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### 9.1.3 Embedding Simple Entailment

The semantics of the RDF vocabulary does not need to be axiomatized for Simple entailment. Nonetheless, the connection between RIF class membership and subclass statements and the RDF type and subclass statements needs axiomatization. We define:

$R^{Simple}$	=	<pre> Document( Group(    Forall ?x ?y (?x[rdf:type -&gt; ?y] :- ?x # ?y)    Forall ?x ?y (?x # ?y :- ?x[rdf:type - &gt; ?y])    Forall ?x ?y (?x[rdfs:subClassOf - &gt; ?y] :- ?x ## ?y)) ) ) </pre>
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The following theorem shows how checking RIF-Simple-entailment of combinations can be reduced to checking entailment of RIF conditions by using the embeddings of RDF graphs defined above.

**Theorem** A list-free [RIF-RDF combination](#)  $C = \langle R, R^{Simple}, \{S_1, \dots, S_n\} \rangle$  [RIF-Simple-entails](#) a [generalized RDF graph](#)  $T$  if and only if  $\text{merge}(\{R, tr_R(S_1), \dots, tr_R(S_n)\})$  [entails](#)  $tr_Q(T)$ ;  $C$  [RIF-Simple-entails](#) a [condition formula](#)  $\phi$  if and only if  $\text{merge}(\{R, R^{Simple}, tr_R(S_1), \dots, tr_R(S_n)\})$  [entails](#)  $\phi$ .

**Proof.** We prove both directions through contraposition. We first consider condition formulas (the second part of the theorem), after which we consider graphs (the first part of the theorem). In the proof we abbreviate  $\text{merge}(\{R, R^{Simple}, tr_R(S_1), \dots, tr_R(S_n)\})$  with  $R'$ .

( $\Rightarrow$ ) Assume  $R'$  does not entail  $\phi$ . This means there is some semantic multi-structure  $\hat{I}$  that is a model of  $R'$ , but not of  $\phi$ . Consider the pair  $(\hat{I}, I)$ , where  $I$  is the interpretation defined as follows:

- $IR$  is  $D_{ind}$ ,
- $IP$  is the set of all  $k$  in  $D_{ind}$  such that there exist some  $a, b$  in  $D_{ind}$  and  $I_{truth}(I_{frame}(a)(k,b)) = t$ ,
- $LV$  is the union of the value spaces of all considered datatypes,

- $IEXT(k)$  is the set of all pairs  $(a, b)$ , with  $a, b$ , and  $k$  in  $D_{ind}$ , such that  $I_{truth}(I_{frame(a)}(k,b))=t$ ,
- $IS(i)$  is  $I_C(\langle i \rangle)$ , for every absolute IRI  $i$  in  $V_U$ , and
- $IL((s, d))$  is  $I_C(\text{tr}("s" \wedge d))$ , for every typed literal  $(s, d)$  in  $V_{TL}$ .

Clearly,  $(\hat{I}, I)$  is a [common-RIF-RDF-interpretation](#): conditions 1-6 in the definition are satisfied by construction of  $I$  and conditions 7 and 8 are satisfied by condition 4 and by the fact that  $\hat{I}$  is a model of  $R^{Simple}$ .

Consider a graph  $S_j$  in  $\{S_1, \dots, S_n\}$ . Let  $x_1, \dots, x_m$  be the blank nodes in  $S_j$  and let  $u_1, \dots, u_m$  be the new IRIs that were obtained from the variables  $?x_1, \dots, ?x_m$  through the skolemization in  $\text{tr}_R(S_j)$ , i.e.,  $u_j = \text{sk}(?x_j)$ . Now, let  $A$  be a mapping from blank nodes to elements in  $D_{ind}$  such that  $A(x_j) = I_C(u_j)$  for every blank node  $x_j$  in  $S_j$ . From the fact that  $I$  is a model of  $\text{tr}_R(S_j)$  and by construction of  $I$  it follows that  $[I+A]$  [satisfies](#)  $S_j$  (see [Section 1.5](#) of [\[RDF-Semantics\]](#)), and so  $I$  satisfies  $S_j$ .

We have that  $\hat{I}$  is a model of  $R$ , by assumption. So,  $(\hat{I}, I)$  satisfies  $C$ . Again, by assumption,  $I$  is not a model of  $\varphi$ . Therefore,  $C$  does not entail  $\varphi$ .

Assume now that  $R'$  does not entail  $\text{tr}_Q(T)$ , which means there is a semantic multi-structure  $\hat{I}'$  that is a model of  $R'$ , but not of  $\text{tr}_Q(T)$ . The common-RIF-RDF-interpretation  $(\hat{I}, I)$  is obtained in the same way as above, and so it satisfies  $C$ .

We proceed by contradiction. Assume  $I$  satisfies  $T$ . This means there is some mapping  $A$  from the blank nodes  $x_1, \dots, x_m$  in  $T$  to objects in  $D_{ind}$  such that  $[I+A]$  satisfies  $T$ . Consider now the semantic multi-structure  $\hat{I}^*$ , which is the same as  $\hat{I}$ , with the exception of the mapping  $I^*_V$  on the variables  $?x_1, \dots, ?x_m$ , which is defined as follows:  $\hat{I}^*_V(?x_j) = A(x_j)$  for each blank node  $x_j$  in  $S$ . By construction of  $I$  and since  $[I+A]$  satisfies  $T$  we can conclude that  $\hat{I}^*$  is a model of  $\text{And}(\text{tr}(t_1) \dots \text{tr}(t_m))$ , and so  $I$  is a model of  $\text{tr}_Q(T)$ , violating the assumption that it is not. Therefore,  $(\hat{I}, I)$  does not satisfy  $T$  and  $C$  does not entail  $T$ .

( $\Leftarrow$ ) Assume  $C$  does not Simple-entail  $\varphi$ . This means there is some common-RIF-RDF-interpretation  $(\hat{I}, I)$  that satisfies  $C$  such that  $I$  is not a model of  $\varphi$ .

Consider the semantic multi-structure  $\hat{I}'$ , which is like  $\hat{I}$ , except for the mapping  $I'_C$  on the new IRIs that were introduced by the skolemization mapping  $\text{sk}()$ . The mapping of these new IRIs is defined as follows: For each graph  $S_j$  in  $\{S_1, \dots, S_n\}$ , let  $x_1, \dots, x_m$  be the blank nodes in  $S_j$  and let  $u_1, \dots, u_m$  be the new IRIs that were obtained from the variables  $?x_1, \dots, ?x_m$  through the skolemization in  $\text{tr}_R(S_j)$ , i.e.,  $u_j = \text{sk}(?x_j)$ . Now, since  $I$  satisfies  $S_j$ , there must be a mapping  $A$  from blank nodes to elements in  $D_{ind}$  such that  $[I+A]$  satisfies  $S_j$ . We define  $I'_C(u_j) = A(x_j)$  for every blank node  $x_j$  in  $S_j$ .

By assumption,  $\hat{I}$  is a model of  $R$  (recall that  $\hat{I}$  differs from  $\hat{I}$  only on the new IRIs, which are not in  $R$ ). Clearly,  $I'$  is also a model of  $R^{Simple}$ , by conditions 7, 8, and 4 in the definition of [common-RIF-RDF-interpretation](#). From the fact that  $I$  satisfies  $S_i$  and by construction of  $I'$  it follows that  $I'$  is a model of  $tr_R(S_i)$ . So,  $I'$  is a model of  $R'$ . Since  $I$  is not a model of  $\varphi$  and  $\varphi$  does not contain any of the new IRIs,  $I'$  is not the model of  $\varphi$ . Therefore,  $R'$  does not entail  $\varphi$ .

Assume now that  $C$  does not entail  $T$ , which means there is a common-RIF-RDF-interpretation  $(\hat{I}, I)$  that satisfies  $C$ , but  $I$  does not satisfy  $T$ . We obtain  $I'$  from  $I$  in the same way as above, and so it satisfies  $R'$ . It can be shown analogous to the ( $\Rightarrow$ ) direction that if  $I'$  is a model of  $tr_Q(T)$ , then there is a blank node mapping  $A$  such that  $[I+A]$  satisfies  $T$ , and thus  $I$  satisfies  $T$ , violating the assumption that it does not. Therefore,  $I'$  is not a model of  $tr_Q(T)$  and thus  $R'$  does not entail  $tr_Q(T)$ .  $\square$

**Theorem** A list-free [RIF-RDF combination](#)  $\langle R, \{S_1, \dots, S_n\} \rangle$  is [satisfiable](#) iff there is a [semantic multi-structure](#)  $\hat{I}$  that is a [model](#) of  $\text{merge}(\{R, R^{Simple}, tr_R(S_1), \dots, tr_R(S_n)\})$ .

**Proof.** The theorem follows immediately from the previous theorem and the observation that a combination (respectively, RIF document) is satisfiable (respectively, has a model) if and only if it does not entail the condition formula " $a = b$ ".  $\square$

#### 9.1.4 Embedding RDF Entailment

We axiomatize the semantics of the RDF vocabulary using the following RIF rules.

To finitely embed RDF entailment, we need to consider a subset of the [RDF axiomatic triples](#). Given a combination  $C$ , the *context* of  $C$  includes  $C$  and its vicinity (i.e., all graphs/formulas considered for entailment checking). The set of *RDF finite-axiomatic triples* is the smallest set such that:

- every RDF axiomatic triple not of the form `rdf:_i rdf:type rdf:Property` is an RDF finite-axiomatic triple, where  $i$  is a positive integer,
- one triple `rdf:_m rdf:type rdf:Property`, for some positive integer  $m$  such that `rdf:_m` does not occur in the context of  $C$ , is an RDF finite-axiomatic triple, and
- if `rdf:_j` occurs in the context of  $C$ , for some positive integer  $j$ , then `rdf:_j rdf:type rdf:Property` is an RDF finite-axiomatic triple.

We assume that the unary predicate symbols `ex:wellxml` and `ex:illxml` are not used in the context of the the given combination.

$R^{RDF}$	=	$\text{merge}((R^{Simple}) \text{ union})$
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	<pre> ((tr(s p o .)) for every RDF finite-axiomatic triple s p o .) union ((ex:illxml(tr("s"^^rdf:XMLLiteral))) for every non-well-typed literal of the form (s, rdf:XMLLiteral) in V<sub>TL</sub>) union ((ex:wellxml(tr("s"^^rdf:XMLLiteral))) for every well-typed literal of the form (s, rdf:XMLLiteral) in V<sub>TL</sub>) union (   Forall ?x (?x[rdf:type -&gt; rdf:Property] :-   Exists ?y ?z (?y[?x -&gt; ?z])),    Forall ?x (?x[rdf:type -&gt; rdf:XMLLiteral] :-   ex:wellxml(?x)),    Forall ?x (rif:error :- And(?x[rdf:type -&gt;   rdf:XMLLiteral] ex:illxml(?x))),    Forall ?x (rif:error :- And(ex:illxml(?x)   Exists ?y (pred:isLiteralOfType(?x ?y))) ) </pre>
--	--

Here, inconsistencies may occur if non-well-typed XML literals, axiomatized using the `ex:illxml` predicate, are in the class extension of `rdf:XMLLiteral`. If this situation occurs, `rif:error` is derived, which signifies an inconsistency in the combination.

**Theorem** An RIF-RDF-satisfiable list-free [RIF-RDF combination](#)  $C = \langle R, \{S_1, \dots, S_n\} \rangle$  [RIF-RDF-entails](#) a [generalized RDF graph](#)  $T$  iff  $\text{merge}(\{R^{RDF}, R, \text{tr}_R(S_1), \dots, \text{tr}_R(S_n)\})$  [entails](#)  $\text{tr}_Q(T)$ .  $C$  [rdf-entails](#) a [condition formula](#)  $\varphi$  iff  $\text{merge}(\{R^{RDF}, R, \text{tr}_R(S_1), \dots, \text{tr}_R(S_n)\})$  [entails](#)  $\varphi$ .

**Proof.** In the proof we abbreviate  $\text{merge}(\{R^{RDF}, R, \text{tr}_R(S_1), \dots, \text{tr}_R(S_n)\})$  with  $R'$ .

The proof is obtained from the [proof of correspondence for Simple entailment](#) in the previous section with the following modifications: (\*) in the ( $\Rightarrow$ ) direction we additionally need to ensure that  $I$  does not satisfy `rif:error`, extend  $I$  to ensure it satisfies the RDF axiomatic triples and show that  $I$  is an RDF-interpretation, and (\*\*) in the ( $\Leftarrow$ ) direction we need to slightly extend the definition of  $I'$  to account for `ex:wellxml` and `ex:illxml`, and show that  $I'$  is a model of  $R^{RDF}$ .

(\*) We assume that, for every non-well-typed literal of the form  $(s, \text{rdf:XMLLiteral})$  in  $V_{TL}$ ,  $I_C(\text{tr}("s"^^\text{rdf:XMLLiteral}))$  is not in the

value space of any of the considered datatypes and  $\text{tr}("s" \wedge \text{rdf:XMLLiteral})[\text{rdf:type} \rightarrow \text{rdf:XMLLiteral}]$  is not satisfied in  $I$ . Since  $C$  is RIF-RDF-satisfiable, one can verify that this does not compromise satisfaction of  $R'$ . Finally, we may assume, without loss of generality, that  $I$  does not satisfy  $\text{rif:error}$ . See also the proof of the following theorem.

For any positive integer  $j$  such that  $\text{rdf:}_j$  does not occur in the context of  $C$ ,  $I$  and  $I$  are extended such that  $\text{IS}(\text{rdf:}_j) = \text{IC}(\text{rdf:}_j) = \text{IC}(\text{rdf:}_m)$  (see the definition of finite-axiomatic triples above for the definition of  $m$ ). Clearly, this does not affect satisfaction of  $R'$  or non-satisfaction of  $\phi$  and  $\text{tr}_Q(T)$ .

To show that  $I$  is an RDF-interpretation, we need to show that  $I$  satisfies the [RDF axiomatic triples](#) and the [RDF semantic conditions](#). Satisfaction of the axiomatic triples follows immediately from the inclusion of  $\text{tr}(t)$  in  $R^{RDF}$  for every RDF finite-axiomatic triple  $t$ , the fact that  $I$  is a model of  $R^{RDF}$ , and construction of  $I$ . Consider the three [RDF semantic conditions](#):

1	$x$ is in IP if and only if $\langle x, I(\text{rdf:Property}) \rangle$ is in $\text{IEXT}(I(\text{rdf:type}))$
2	<p>If <math>"xxx" \wedge \text{rdf:XMLLiteral}</math> is in <math>V</math> and <math>xxx</math> is a well-typed XML literal string, then</p> <p>(a) <math>\text{IL}("xxx" \wedge \text{rdf:XMLLiteral})</math> is the XML value of <math>xxx</math>;            (b) <math>\text{IL}("xxx" \wedge \text{rdf:XMLLiteral})</math> is in <math>LV</math>;            (c) <math>\text{IEXT}(I(\text{rdf:type}))</math> contains <math>\langle \text{IL}("xxx" \wedge \text{rdf:XMLLiteral}), I(\text{rdf:XMLLiteral}) \rangle</math></p>
3	<p>If <math>"xxx" \wedge \text{rdf:XMLLiteral}</math> is in <math>V</math> and <math>xxx</math> is an ill-typed XML literal string, then</p> <p>(a) <math>\text{IL}("xxx" \wedge \text{rdf:XMLLiteral})</math> is not in <math>LV</math>;            (b) <math>\text{IEXT}(I(\text{rdf:type}))</math> does not contain <math>\langle \text{IL}("xxx" \wedge \text{rdf:XMLLiteral}), I(\text{rdf:XMLLiteral}) \rangle</math>.</p>

Satisfaction of condition 1 follows from satisfaction of the first rule in  $R^{RDF}$  in  $I$  and construction of  $I$ ; specifically, the second bullet in the definition.

Consider a well-typed XML literal  $"xxx" \wedge \text{rdf:XMLLiteral}$ . By the definition of satisfaction in RIF BLD,  $\text{IC}("xxx" \wedge \text{rdf:XMLLiteral})$  is the XML value of  $xxx$  (condition 2a), and is clearly in  $LV$  (condition 2b), by definition of  $I$ . Condition 2c is satisfied by satisfaction of the second rule in  $R^{RDF}$  in  $I$ .

Satisfaction of 3a and 3b follows straightforwardly from our assumptions on  $I$ . This establishes the fact that  $I$  is an RDF-interpretation.

(\*\*) Recall that, by assumption, `ex:wellxml` and `ex:illxml` are not used in  $R$ . Therefore, changing satisfaction of atomic formulas involving `ex:wellxml` and `ex:illxml` does not affect satisfaction of  $R$ . We assume that  $I'_C(\text{ex:wellxml})=k$  and  $I'_C(\text{ex:illxml})=l$  are distinct unique elements, i.e., no other constants is mapped to  $k$  and  $l$ .

We define  $I'_F(k)$  and  $I'_F(l)$  as follows: For every typed literal of the form  $(s, \text{rdf:XMLLiteral})$  such that  $I'_C(\text{tr}(s^{\wedge}\text{rdf:XMLLiteral}))=u$ , if  $(s, \text{rdf:XMLLiteral})$  is well-typed,  $I_{\text{truth}}(I'_F(k)(u))=t$  and  $I_{\text{truth}}(I'_F(l)(u))=f$ , otherwise  $I_{\text{truth}}(I'_F(k)(u))=f$  and  $I_{\text{truth}}(I'_F(l)(u))=t$ ;

$I_{\text{truth}}(I'_F(k)(v))=I_{\text{truth}}(I'_F(l)(v))=f$  for every other object  $v$  in  $D_{\text{ind}}$ .

Consider  $R^{RDF}$ . Satisfaction of  $R^{\text{Simple}}$  was established in the proof in the previous section. Satisfaction of the facts corresponding to the RDF axiomatic triples in  $I'$  follows immediately from the definition of [common-RIF-RDF-interpretation](#) and the fact that  $I$  is an RDF-interpretation, and thus satisfies all RDF axiomatic triples.

Satisfaction of the `ex:wellxml` and `ex:illxml` facts in  $R^{RDF}$  follows immediately from the definition of  $I'$ . Finally, satisfaction of the rules in  $R^{RDF}$  follow straightforwardly from the RDF semantic conditions 1, 2, and 3. This establishes the fact that  $I'$  is a model of  $R^{RDF}$ .  $\square$

**Theorem** A list-free [RIF-RDF combination](#)  $\langle R, \{S_1, \dots, S_n\} \rangle$  is [RIF-RDF-satisfiable](#) iff  $\text{merge}(\{R^{RDF}, R, \text{tr}_R(S_1), \dots, \text{tr}_R(S_n)\})$  does not [entail](#) `rif:error`.

**Proof.** Recall that we assume `rif:error` does not occur in  $R$ . If  $\langle R, \{S_1, \dots, S_n\} \rangle$  is not RIF-RDF-satisfiable, then either  $\text{merge}(\{R, \text{tr}_R(S_1), \dots, \text{tr}_R(S_n)\})$  is not consistent, or condition 3a or 3b (see previous proof) is violated. In either case, `rif:error` is entailed. If `rif:error` is entailed, either  $\text{merge}(\{R^{RDF}, R, \text{tr}_R(S_1), \dots, \text{tr}_R(S_n)\})$  is inconsistent, which means  $\text{merge}(\{R, \text{tr}_R(S_1), \dots, \text{tr}_R(S_n)\})$  is not consistent and thus  $\langle R, \{S_1, \dots, S_n\} \rangle$  is not RIF-RDF-satisfiable, or the body of the second or third rule in  $R^{RDF}$  is satisfied in every model, which means either condition 3a or 3b is violated, and so  $\langle R, \{S_1, \dots, S_n\} \rangle$  is not RIF-RDF-satisfiable.  $\square$

### 9.1.5 Embedding RDFS Entailment

We axiomatize the semantics of the RDF(S) vocabulary using the following RIF rules.

Similar to the RDF case, the set of *RDFS finite-axiomatic triples* is the smallest set such that:

- every [RDFS axiomatic triple](#) not of the form `rdf:_i ...`, where *i* is a positive integer, is an RDFS finite-axiomatic triple,
- the triples `rdf:_m rdf:type rdfs:ContainerMembershipProperty`, `rdf:_m rdfs:domain rdfs:Resource`, and `rdf:_m rdfs:range rdfs:Resource`, for some positive integer *m* such that `rdf:_m` does not occur in the context of *C*, are RDFS finite-axiomatic triples, and
- if `rdf:_j` occurs in the context of the combination *C*, for some positive integer *j*, then `rdf:_j rdf:type rdfs:ContainerMembershipProperty`, `rdf:_j rdfs:domain rdfs:Resource`, and `rdf:_j rdfs:range rdfs:Resource` are RDFS finite-axiomatic triples.

We assume that the unary predicate symbol `ex:welllit` is not used in the context of the given combination.

$R^{RDFS}$	=	<pre> merge(<math>(R^{RDF})</math> union ((tr(s p o .) for every RDFS finite-axiomatic triple s p o .) union ((ex:welllit("s"^^u) for every well-typed literal (s,u) in <math>V_{TL}</math>) union ((sk(tr(s))[rdf:type -&gt; rdfs:Resource) for every name or blank node s) union (   Forall ?x (?x[rdf:type -&gt; rdfs:Resource] :-   Exists ?y ?z (?x[?y -&gt; ?z])),    Forall ?x (?x[rdf:type -&gt; rdfs:Resource] :-   Exists ?y ?z (?z[?y -&gt; ?x])),    Forall ?u ?v ?x ?y (?u[rdf:type -&gt; ?y] :-   And(?x[rdfs:domain -&gt; ?y] ?u[?x -&gt; ?v])),    Forall ?u ?v ?x ?y (?v[rdf:type -&gt; ?y] :-   And(?x[rdfs:range -&gt; ?y] ?u[?x -&gt; ?v])),    Forall ?x (?x[rdfs:subPropertyOf -   &gt; ?x] :- ?x[rdf:type -&gt; rdf:Property]),    Forall ?x ?y ?z (?x[rdfs:subPropertyOf -   &gt; ?z] :- And (?x[rdfs:subPropertyOf -   &gt; ?y] ?y[rdfs:subPropertyOf -&gt; ?z])),    Forall ?x ?y ?z1 ?z2 (?z1[?y -&gt; ?z2] :- And   (?x[rdfs:subPropertyOf -&gt; ?y] ?z1[?x -   &gt; ?z2])), </pre>
------------	---	---

```

Forall ?x (?x[rdfs:subClassOf ->
rdfs:Resource] :- ?x[rdf:type ->
rdfs:Class]),

Forall ?x ?y ?z (?z[rdf:type -> ?y] :- And
(?x[rdfs:subClassOf -> ?y] ?z[rdf:type -
> ?x])),

Forall ?x (?x[rdfs:subClassOf -
> ?x] :- ?x[rdf:type -> rdfs:Class]),

Forall ?x ?y ?z (?x[rdfs:subClassOf -
> ?z] :- And (?x[rdfs:subClassOf -
> ?y] ?y[rdfs:subClassOf -> ?z])),

Forall ?x (?x[rdfs:subPropertyOf ->
rdfs:member] :- ?x[rdf:type ->
rdfs:ContainerMembershipProperty]),

Forall ?x (?x[rdfs:subClassOf ->
rdfs:Literal] :- ?x[rdf:type ->
rdfs:Datatype]),

Forall ?x (rif:error :- And(?x[rdf:type ->
rdfs:Literal] ex:illxml(?x)))

Forall ?x (?x[rdf:type -> rdfs:Literal] :-
ex:welllit(?x))

)

```

In the following theorems it is assumed that, in combinations  $C=\langle R,\{S_1,\dots,S_n\rangle$ ,  $R$  does not have mentions of `rdfs:Resource`,  $S_1,\dots,S_n$  do not have mentions of `rdfs:Resource` beyond triples of the form `xxx rdf:type rdfs:Resource`, and entailed graphs  $T$  and formulas  $\varphi$  do not have mentions of `rdfs:Resource`.

**Theorem** An RIF-RDFS-satisfiable list-free [RIF-RDF combination](#)  $C=\langle R,\{S_1,\dots,S_n\rangle$  [RIF-RDFS-entails](#) a [generalized RDF graph](#)  $T$  if and only if  $\text{merge}(\{R, R^{RDFS}, \text{tr}(S_1), \dots, \text{tr}(S_n)\})$  [entails](#)  $\text{tr}(T)$ ;  $C$  [RIF-RDFS-entails](#) a [condition formula](#)  $\varphi$  if and only if  $\text{merge}(\{R, R^{RDFS}, \text{tr}(S_1), \dots, \text{tr}(S_n)\})$  [entails](#)  $\varphi$ .

**Theorem** A list-free [RIF-RDF combination](#)  $\langle R,\{S_1,\dots,S_n\rangle$  is [RIF-RDFS-satisfiable](#) if and only if  $\text{merge}(\{R, R^{RDFS}, \text{tr}(S_1), \dots, \text{tr}(S_n)\})$  does not entail `rif:error`.

## 9.2 Embedding RIF-OWL 2 RL Combinations

It is known that expressive Description Logic languages such as OWL 2 DL cannot be straightforwardly embedded into typical rules languages such as RIF BLD [RIF-BLD], because of features such as disjunction and negation.

In this section we consider a subset of OWL 2 DL in RIF-OWL DL combinations, namely, the OWL 2 RL profile [OWL2-Profiles], and show how reasoning with RIF-OWL 2 RL combinations can be reduced to reasoning with RIF.

The embedding of RIF-OWL 2 RL combinations is not defined for combinations that include infinite OWL ontologies and for combinations that include ontologies with RDF URI references that are not absolute IRIs or plain literals that are not in the lexical space of the `xs:string` datatype. In addition, the guard predicate `pred:is-dt` [DTB] must be defined for each datatype used in the combination, where *dt* is the short name of the datatype.

Since OWL 2 RL includes equality through `ObjectMaxCardinality` and `DataMaxCardinality` restrictions, as well as `FunctionalObjectProperty` `UniverseFunctionalObjectProperty`, `SameIndividual`, and `HasKey` axioms, and there is non-trivial interaction between such equality and the predicates in the RIF rules in the combination, embedding RIF-OWL 2 RL combinations into RIF requires equality. Therefore, the embedding presented in this appendix is not in RIF Core, even if the RIF document in the combination is. If the ontologies in the combination do not contain any of the mentioned constructs, the embedding is in Core. Also, it is well-known that adding equality to a rules language does not increase its expressiveness in the absence of function symbols: one can replace equality = with a new binary predicate symbol, and add rules for reflexivity and the principle of substitutivity (also called the replacement property).

### 9.2.1 Embedding RIF DL-document formulas into RIF BLD

Recall that the semantics of frame formulas in [DL-document formulas](#) is different from the semantics of frame formulas in RIF documents. Nonetheless, DL-document formulas can be embedded into RIF documents, by translating frame formulas to predicate formulas. The mapping *tr* is the identity mapping on all RIF formulas, with the exception of frame formulas, as defined in the following table.

In the table, the mapping *tr'* is an injective function that maps constants to new constants, i.e., constants that are not used in the original document or its vicinity (i.e., entailed or entailing formula). It "generates" a new constant from an existing one.

Mapping RIF DL-document formulas to RIF documents.

RIF Construct	Mapping
Term <i>t</i>	$tr(t)=t$

Atomic formula $\varphi$ that is not a frame formula	$\text{tr}(\varphi)=\varphi$
$a[b_1 \rightarrow c_1 \dots b_n \rightarrow c_n]$ , with $n \geq 2$	$\text{tr}(a[b_1 \rightarrow c_1 \dots b_n \rightarrow c_n]) = \text{And}(\text{tr}(a[b_1 \rightarrow c_1]) \dots \text{tr}(a[b_n \rightarrow c_n]))$
$a[b \rightarrow c]$ , where $a$ and $c$ are terms and $b \neq \text{rdf:type}$ is a constant	$\text{tr}(a[b \rightarrow c]) = \text{tr}'(b)(a \ c)$
$a[\text{rdf:type} \rightarrow c]$ , where $a$ is a term and $c$ is a constant	$\text{tr}(a[\text{rdf:type} \rightarrow c]) = \text{tr}'(c)(a)$
Exists ?V1 ... ?Vn( $\varphi$ )	$\text{tr}(\text{Exists ?V1} \dots \text{?Vn}(\varphi)) = \text{Exists ?V1} \dots \text{?Vn}(\text{tr}(\varphi))$
And( $\varphi_1 \dots \varphi_n$ )	$\text{tr}(\text{And}(\varphi_1 \dots \varphi_n)) = \text{And}(\text{tr}(\varphi_1) \dots \text{tr}(\varphi_n))$
Or( $\varphi_1 \dots \varphi_n$ )	$\text{tr}(\text{Or}(\varphi_1 \dots \varphi_n)) = \text{Or}(\text{tr}(\varphi_1) \dots \text{tr}(\varphi_n))$
$\varphi_1 :- \varphi_2$	$\text{tr}(\varphi_1 :- \varphi_2) = \text{tr}(\varphi_1) :- \text{tr}(\varphi_2)$
Forall ?V1 ... ?Vn( $\varphi$ )	$\text{tr}(\text{Forall ?V1} \dots \text{?Vn}(\varphi)) = \text{Forall ?V1} \dots \text{?Vn}(\text{tr}(\varphi))$
Group( $\varphi_1 \dots \varphi_n$ )	$\text{tr}(\text{Group}(\varphi_1 \dots \varphi_n)) = \text{Group}(\text{tr}(\varphi_1) \dots \text{tr}(\varphi_n))$
Document( <i>directive</i> <sub>1</sub> ... <i>directive</i> <sub>n</sub> $\Gamma$ )	$\text{tr}(\text{Document}(\textit{directive}_1 \dots \textit{directive}_n \ \Gamma)) = \text{Document}(\textit{directive}_1 \dots \textit{directive}_n \ \text{tr}(\Gamma))$

For the purpose of making statements about this embedding, we define a notion of entailment for DL-document formulas.

**Definition.** A [RIF-BLD DL-document formula](#)  $R$  **dl-entails** a [DL-condition](#)  $\varphi$  if for every dl-semantic multi-structure  $\hat{I}$  that is a [model](#) of  $R$  it holds that  $\text{TVaI}(\varphi) = \mathbf{t}$ .  $\square$

The following lemma establishes faithfulness with respect to entailment of the embedding.

**RIF-BLD DL-document formula Lemma** A [RIF-BLD DL-document formula](#)  $R$  **dl-entails** a [DL-condition](#)  $\varphi$  if and only if  $\text{tr}(R)$  **entails**  $\text{tr}(\varphi)$ .

**Proof.** We prove both directions by contradiction: if the entailment does not hold on the one side, we show that it also does not hold on the other.

( $\Rightarrow$ ) Assume  $\text{tr}(R)$  does not entail  $\text{tr}(\varphi)$ . This means there is some semantic multi-structure  $I = \langle TV, DTS, D, D_{\text{ind}}, D_{\text{func}}, IC, IV, IF, I_{\text{frame}}, I_{\text{SF}}, I_{\text{sub}}, I_{\text{isa}}, I_{\text{=}}, I_{\text{external}}, I_{\text{truth}} \rangle$  that is a model of  $\text{tr}(R)$ , but not of  $\text{tr}(\varphi)$ . Consider the dl-semantic multi-structure  $I^* = \langle TV, DTS, D, D_{\text{ind}}, D_{\text{func}}, I^*C, IV, IF, I^*_{\text{frame}}, I_{\text{SF}}, I_{\text{sub}}, I_{\text{isa}}, I_{\text{=}}, I_{\text{external}}, I_{\text{truth}} \rangle$ , with  $I^*C$  and  $I^*_{\text{frame}}$  defined as follows: Let  $t$  be an element in  $D$  such that  $I_{\text{truth}}(t) = t$  and let  $f$  in  $D$  be such that  $I_{\text{truth}}(f) = f$ .

- for every constant  $c'$  used as unary or binary predicate symbol in  $\text{tr}(R)$  or  $\text{tr}(\varphi)$  such that  $c' = \text{tr}'(c)$  for some constant  $c$ ,  $I^*C(c') = IC(c)$ ;  $I^*C(c^*) = I^*C(c^*)$  for every other constant  $c^*$ ;
- for every constant  $c'$  used as unary predicate symbol in  $\text{tr}(R)$  or  $\text{tr}(\varphi)$  such that  $c' = \text{tr}'(c)$  for some constant  $c$ , and every object  $k$  in  $D_{\text{ind}}$ , if  $I_{\text{truth}}(IF(IC(c'))(k)) = t$ ,  $I^*_{\text{frame}}(k)(IC(\text{rdf:type}), IC(c)) = t$ ,
- for every constant  $b'$  used as binary predicate symbol in  $\text{tr}(R)$  or  $\text{tr}(\varphi)$  such that  $b' = \text{tr}'(b)$  for some constant  $b$ , and every pair  $(k, l)$  in  $D_{\text{ind}} \times D_{\text{ind}}$ , if  $I_{\text{truth}}(IF(IC(b'))(k, l)) = t$ ,  $I^*_{\text{frame}}(k)(IC(b), l) = t$ ,
- if  $I^*_{\text{frame}}(k)((b_1, \dots, b_n)) = t$  and  $I^*_{\text{frame}}(k)((c_1, \dots, c_m)) = t$  for any two finite bags  $(b_1, \dots, b_n)$  and  $(c_1, \dots, c_m)$ , then  $I^*_{\text{frame}}(k)((b_1, \dots, b_n, c_1, \dots, c_m)) = t$ , and
- $I^*_{\text{frame}}(b) = f$  for any other bag  $b$ .

Observe that  $\text{tr}(R)$  and  $\text{tr}(\varphi)$  do not include frame formulas.

To show that  $I^*$  is a model of  $R$  and not of  $\varphi$ , we only need to show that (+) for any frame formula  $a[b \rightarrow c]$  that is a DL-condition,  $I^*$  is a model of  $a[b \rightarrow c]$  iff  $I$  is a model of  $\text{tr}(a[b \rightarrow c])$ . This argument straightforwardly extends to the case of frames with multiple  $b_i$ s and  $c_i$ s, since in RIF semantic structures the following condition is required to hold:  $TVal_I(a[b_1 \rightarrow c_1 \dots b_n \rightarrow c_n]) = t$  if and only if  $TVal_I(a[b_1 \rightarrow c_1]) = \dots = TVal_I(a[b_n \rightarrow c_n]) = t$  [RIF-BLD].

Consider the case  $b = \text{rdf:type}$ . Then,

$I^*$  is a model of  $a[b \rightarrow c]$  iff  $I_{\text{truth}}(I^*_{\text{frame}}(I(a))(IC(\text{rdf:type}), IC(c))) = t$ .

From the definition of  $I^*$  we obtain

$I_{\text{truth}}(I^*_{\text{frame}}(I(a))(IC(\text{rdf:type}), IC(c))) = t$  iff

$I^*_{\text{frame}}(I(a))(IC(\text{rdf:type}), IC(c)) = t$ .

By definition of the embedding, we know that  $\text{tr}'(c)$  is used as unary

predicate symbol in  $\text{tr}(R)$  or  $\text{tr}(\varphi)$ . From the definition of  $I^*$  we obtain

$I^*_{\text{frame}}(I(a))(IC(\text{rdf:type}), IC(c)) = t$  iff  $I_{\text{truth}}(IF(IC(\text{tr}'(c)))(I(a))) = t$ .

Finally, since  $\text{tr}(a[b \rightarrow c]) = \text{tr}'(c)(a)$ , we obtain

$I_{\text{truth}}(IF(IC(\text{tr}'(c)))(I(a))) = t$  iff  $I$  is a model of  $\text{tr}(a[b \rightarrow c])$ .

From this chain of equivalences follows that  $I^*$  is a model of  $a[b \rightarrow c]$

iff  $I$  is a model of  $\text{tr}(a[b \rightarrow c])$ .

The argument for the case  $b \neq \text{rdf:type}$  is analogous, thereby obtaining (+).

( $\Leftarrow$ ) Assume  $R$  does not dl-entail  $\varphi$ . This means there is some dl-semantic multi-structure  $I = \langle TV, DTS, D, D_{\text{ind}}, D_{\text{func}}, IC, IV, IF, I_{\text{frame}}, ISF, I_{\text{sub}}, I_{\text{isa}}, I_{\text{=}}, I_{\text{external}}, I_{\text{truth}} \rangle$  that is a model of  $R$ , but not of  $\varphi$ . Let  $B$  be the set of constant symbols occurring in the frame formulas of the forms  $a[\text{rdf:type} \rightarrow b]$  and  $a[b \rightarrow c]$  in  $R$  or  $\varphi$ .

Consider the semantic multi-structure  $I^* = \langle TV, DTS, D, D_{\text{ind}}, D_{\text{func}}, I^*_C, IV, I^*_F, I^*_{\text{frame}}, ISF, I_{\text{sub}}, I_{\text{isa}}, I_{\text{=}}, I_{\text{external}}, I_{\text{truth}} \rangle$ . Let  $t$  and  $f$  in  $D$  be such that  $I_{\text{truth}}(t) = \mathbf{t}$  and  $I_{\text{truth}}(f) = \mathbf{f}$ . We define  $I^*_C$ ,  $I^*_{\text{frame}}$ , and  $I^*_F$  as follows:

- $I^*_C(\text{tr}(b)) = I^*_C(b)$  for any  $b$  in  $B$ ;  $I^*_C(c) = IC(c)$  for any  $c$  not in  $B$ ,
- $I^*_{\text{frame}}(b) = f$  for any finite bag  $b$  of  $D$ , and
- $I^*_F$  is defined as follows:
  - for every  $c$  in  $B$ , given an object  $k$  in  $D_{\text{ind}}$ , if  $I_{\text{truth}}(I_{\text{frame}}(k)(IC(\text{rdf:type}), IC(c))) = \mathbf{t}$ ,  $I^*_F(I^*_C(\text{tr}(c)))(k) = t$ ;  $I^*_F(I^*_C(\text{tr}(c)))(k') = f$  for any other  $k'$  in  $D_{\text{ind}}$ ,
  - for every  $b$  in  $B$ , given a pair  $(k, l)$  in  $D_{\text{ind}} \times D_{\text{ind}}$ , if  $I_{\text{truth}}(I_{\text{frame}}(k)(IC(b), l)) = \mathbf{t}$ ,  $I^*_F(\text{tr}(b))(k, l) = t$ ;  $I^*_F(\text{tr}(b))(k', l') = f$  for any other pair  $(k', l')$  in  $D_{\text{ind}} \times D_{\text{ind}}$ , and
  - $I^*_F(c') = I_F(c')$  for every other constant  $c'$ .

Observe that  $R$  and  $\varphi$  do not include predicate formulas involving derived constant symbols  $\text{tr}(b)$  or  $\text{tr}(c)$ . The remainder of the proof is analogous to the ( $\Rightarrow$ ) direction.  $\square$

### 9.2.2 Embedding OWL 2 RL into RIF BLD

The embedding of OWL 2 RL into RIF BLD has two stages: normalization and embedding.

The OWL 2 syntax is given in terms of a structural model, and there is a functional-style syntax that is a serialization of this structural model. For convenience, normalization and embedding in this section are done in terms of the functional-style syntax. That is, the normalization mapping takes as input a functional-style syntax ontology document and produces a normalized ontology document. The embedding mapping takes as input a normalized ontology document and produces an RIF document. We refer to [Section 4.2](#) of [\[OWL2-Profiles\]](#) for the specification of the OWL 2 RL syntax.

### 9.2.2.1 Normalization of OWL 2 RL

Normalization splits the OWL axioms so that the later mapping to RIF of the individual axioms results in rules. Additionally, it simplifies the axioms and removes annotations.

It is assumed that the normalization process is preceded by a simplification process that removes all namespace prefixes, turns all CURIEs and relative IRIs into absolute IRIs, and removes all annotations, import statements, entity declarations, and annotation axioms.

We note here that, strictly speaking, simplified OWL 2 RL ontologies are not OWL 2 RL ontologies in the general case, because certain entity declarations are required (e.g., those distinguishing data from object properties). It is assumed that such entity declarations are present implicitly, i.e., they do not appear explicitly in the simplified ontology, but they are known. We also note that removing import statements in the simplification does not prohibit importing ontologies in practice; since combinations contain sets of ontologies, all imported ontologies may be added to these sets. The normalization mapping  $tr_N$  takes as input a simplified ontology  $O$  and produces an equivalent normalized ontology  $O'$ .

The names of variables used in the mapping generally correspond to the names of productions in the [OWL 2 RL grammar](#).

Normalization of OWL 2 RL ontolo

#	Statement	Normaliz
1	<pre>trN(   Ontology( [ ontologyIRI [ versionIRI ]   ]   axiom<sub>1</sub>   ...   axiom<sub>n</sub> ) )</pre>	<pre>Ontology( trN(axiom<sub>1</sub>) ... trN(axiom<sub>n</sub>) )</pre>
2	<pre>trN(   SubClassOf (subClassExpression   ...ObjectIntersectionOf (     superClassExpression<sub>1</sub>     ...     superClassExpression<sub>n</sub>   ) ...) )</pre>	<pre>trN(SubClassOf (subClassExpre ...superClassExpression<sub>1</sub>... ... trN(SubClassOf (subClassExpre ...superClassExpression<sub>n</sub>...</pre>

3	<code>trN(   SubClassOf (subClassExpression<sub>1</sub>     ObjectComplementOf (subClassExpression<sub>1</sub>)) )</code>	<code>trN(SubClassOf (ObjectInterse   subClassExpression<sub>2</sub>) owl:No</code>
4	<code>trN(SubClassOf (subClassExpression X))</code>	<code>SubClassOf (subClassExpressi</code>
5	<code>trN(   EquivalentClasses (     equivClassExpression<sub>1</sub>     ...     equivClassExpression<sub>m</sub> ) )</code>	<code>trN(SubClassOf (equivClassExp   ...   trN(SubClassOf (equivClassExp     equivClassExpression<sub>m</sub> )   trN(SubClassOf (equivClassExp</code>
6	<code>trN(   DisjointClasses (     subClassExpression<sub>1</sub>     ...     subClassExpression<sub>m</sub> ) )</code>	<code>trN(SubClassOf (ObjectInterse   subClassExpression<sub>2</sub>) owl:No   ...   trN(SubClassOf (ObjectInterse     subClassExpression<sub>m</sub>) owl:No   ...   trN(SubClassOf (ObjectInterse     subClassExpression<sub>m</sub>) owl:No</code>
7	<code>trN(   SubObjectPropertyOf (     subPropertyExpression     superPropertyExpression ) )</code>	<code>SubObjectPropertyOf (   subPropertyExpression   superPropertyExpression )</code>
8	<code>trN(   SubDataPropertyOf (     subPropertyExpression     superPropertyExpression ) )</code>	<code>SubDataPropertyOf (   subPropertyExpression   superPropertyExpression )</code>

9	<pre>trN(   EquivalentObjectProperties (     ObjectPropertyExpression<sub>1</sub>     ...     ObjectPropertyExpression<sub>m</sub> ) )</pre>	<pre>trN(SubObjectPropertyOf (ObjectPropertyExpression<sub>2</sub>)   ... trN(SubObjectPropertyOf (ObjectPropertyExpression<sub>m</sub>) trN(SubObjectPropertyOf (ObjectPropertyExpression<sub>1</sub>))</pre>
10	<pre>trN(   EquivalentDataProperties (     DataPropertyExpression<sub>1</sub>     ...     DataPropertyExpression<sub>m</sub> ) )</pre>	<pre>trN(SubDataPropertyOf (DataPropertyExpression<sub>2</sub>)   ... trN(SubDataPropertyOf (DataPropertyExpression<sub>m</sub>) trN(SubDataPropertyOf (DataPropertyExpression<sub>1</sub>))</pre>
11	<pre>trN(   DisjointObjectProperties (     ObjectPropertyExpression<sub>1</sub>     ...     ObjectPropertyExpression<sub>m</sub> ) )</pre>	<pre>DisjointObjectProperties (ObjectPropertyExpression<sub>2</sub>)   ... DisjointObjectProperties (ObjectPropertyExpression<sub>m</sub>)   ... DisjointObjectProperties (ObjectPropertyExpression<sub>m</sub>)</pre>
12	<pre>trN(   DisjointDataProperties (     DataPropertyExpression<sub>1</sub>     ...     DataPropertyExpression<sub>m</sub> ) )</pre>	<pre>DisjointDataProperties (DataPropertyExpression<sub>2</sub>)   ... DisjointDataProperties (DataPropertyExpression<sub>m</sub>)   ... DisjointDataProperties (DataPropertyExpression<sub>m</sub>)</pre>
13	<pre>trN(   InverseObjectProperties (     PropertyExpression<sub>1</sub>     PropertyExpression<sub>2</sub> ) )</pre>	<pre>InverseObjectProperties (   PropertyExpression<sub>1</sub>   PropertyExpression<sub>2</sub> )</pre>

14	<pre>trN(   ObjectPropertyDomain (     PropertyExpression     superClassExpression ) )</pre>	<pre>trN(SubClassOf (   ObjectSomeValuesFrom (Prope   superClassExpression )</pre>
15	<pre>trN(   DataPropertyDomain (     DataProperty     superClassExpression ) )</pre>	<pre>trN(SubClassOf (   ObjectSomeValuesFrom (DataP   superClassExpression )</pre>
16	<pre>trN(   ObjectPropertyRange (     ObjectInverseOf (Property)     superClassExpression ) )</pre>	<pre>trN(SubClassOf (   ObjectSomeValuesFrom (Prope   superClassExpression )</pre>
17	<pre>trN(   ObjectPropertyRange (     Property     superClassExpression ) )</pre>	<pre>trN(SubClassOf (   ObjectSomeValuesFrom (Objec   superClassExpression )</pre>
18	<pre>trN(   DataPropertyRange (     DataProperty     superClassExpression ) )</pre>	<pre>trN(SubClassOf (   owl:Thing   DataAllValuesFrom (DataProp</pre>
19	<pre>trN(   FunctionalObjectProperty (     PropertyExpression ) )</pre>	<pre>FunctionalObjectProperty (   PropertyExpression )</pre>
20	<pre>trN(</pre>	<pre>FunctionalDataProperty (</pre>

	<pre>FunctionalDataProperty(   DataProperty ) )</pre>	<pre>DataProperty )</pre>
21	<pre>trN( InverseFunctionalObjectProperty(   PropertyExpression ) )</pre>	<pre>InverseFunctionalObjectProp PropertyExpression )</pre>
22	<pre>trN( IrreflexiveObjectProperty(   PropertyExpression ) )</pre>	<pre>IrreflexiveObjectProperty(   PropertyExpression )</pre>
23	<pre>trN( SymmetricObjectProperty(   PropertyExpression ) )</pre>	<pre>SymmetricObjectProperty(   PropertyExpression )</pre>
24	<pre>trN( AsymmetricObjectProperty(   PropertyExpression ) )</pre>	<pre>AsymmetricObjectProperty(   PropertyExpression )</pre>
25	<pre>trN( TransitiveObjectProperty(   PropertyExpression ) )</pre>	<pre>TransitiveObjectProperty(   PropertyExpression )</pre>
26	<pre>trN( DatatypeDefinition( ... ) )</pre>	<pre>DatatypeDefinition( ... )</pre>
27	<pre>trN( HasKey( ... )</pre>	<pre>HasKey( ... )</pre>

	)	
28	<pre>trN(   SameIndividual (     Individual<sub>1</sub>     ...     Individual<sub>m</sub>) )</pre>	<pre>SameIndividual (Individual<sub>1</sub> ... SameIndividual (Individual<sub>m</sub>- SameIndividual (Individual<sub>m</sub></pre>
29	<pre>trN(   DifferentIndividuals (     Individual<sub>1</sub>     ...     Individual<sub>m</sub>) )</pre>	<pre>DifferentIndividuals (Indivi &lt;tt&gt; ... SameIndividual (Individual<sub>1</sub> ... SameIndividual (Individual<sub>m</sub>-</pre>
30	<pre>trN(   ClassAssertion (     superClassExpression     Individual) )</pre>	<pre>SubClassOf (ObjectOneOf ( Ind )</pre>
31	<pre>trN(   ObjectPropertyAssertion (     ObjectPropertyExpression     source     target) )</pre>	<pre>SubClassOf (ObjectOneOf ( sou ObjectHasValue (ObjectProper</pre>
32	<pre>trN(   NegativeObjectPropertyAssertion (     ObjectPropertyExpression     source     target) )</pre>	<pre>SubClassOf (ObjectOneOf ( sou ObjectComplementOf (ObjectHa target) ) )</pre>
33	<pre>trN(</pre>	<pre>SubClassOf (ObjectOneOf ( sou target) )</pre>

	<pre>DataPropertyAssertion (   DataProperty   source   target) )</pre>	
34	<pre>trN(   NegativeDataPropertyAssertion (     DataProperty     source     target) )</pre>	<pre>SubClassOf (ObjectOneOf ( sou ObjectComplementOf (DataHasV</pre>

We note that normalized OWL 2 RL ontologies are not necessarily OWL 2 RL ontologies, since `owl:Thing` may appear in subclass expressions, as a result of the transformation of `DataPropertyRange` axioms.

The following lemma establishes the fact that, for the purpose of entailment, the ontologies in a combination may be replaced with their normalization.

**Normalization Lemma** Given a combination  $C = \langle R, \{O_1, \dots, O_n\} \rangle$ , where  $O_1, \dots, O_n$  are simplified OWL 2 RL ontologies that do not import ontologies,  $C$  RIF-OWL DL-entails  $\phi$  iff  $C' = \langle R, \{trN(O_1), \dots, trN(O_n)\} \rangle$  RIF-OWL DL-entails  $\phi$ .

### 9.2.2.2 Embedding Normalized OWL 2 RL

We now proceed with the embedding of normalized OWL 2 RL ontologies into RIF DL-document formulas. The embedding function  $tr_O$  takes as input a normalized OWL 2 RL ontology and returns a RIF-BLD DL-document formula. The embeddings of IRIs and literals is as defined in the Section [Embedding Symbols](#).

When we speak about class IDs and datatype IDs we mean IRIs used as identifiers for classes, respectively datatypes. By the syntactic restrictions on OWL ontologies, these sets are disjoint. Similarly, we speak about data, object, and annotation property IDs when talking about IRIs used as identifiers for data, object, respectively annotation properties. These sets of property identifiers are mutually disjoint for any OWL ontology.

#	Normalized OWL	Embedding Normalized
1	$tr_O($	Document

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	<pre>Ontology(   axiom<sub>1</sub>   ...   axiom<sub>n</sub> ) )</pre>	<pre>tro(axiom<sub>1</sub> ... tro(axiom<sub>n</sub> ))</pre>
2	<pre>tro(   SubClassOf(subClassExpression superClassExpression) )</pre>	<pre>tro(subCl</pre>
3	<pre>tro(subClassExpression, [Object Data]AllValuesFrom(property<sub>1</sub> ...[Object Data]AllValuesFrom(property<sub>n</sub> X) ...),?x)</pre>	<pre>Forall ? tro(subCl ?x[tr(prop &gt; ?y<sub>2</sub>) ... ?y<sub>n-1</sub>[tr</pre>
4	<pre>tro(subClassExpression, [Object Data]AllValuesFrom(property<sub>1</sub> ...AllValuesFrom(property<sub>n</sub> MaxCardinality(0 PropertyExpression ClassExpression) ...),?x)</pre>	<pre>Forall ? tro(subCl ?x[tr(prop &gt; ?y<sub>2</sub>) ... ?y<sub>n-1</sub>[tr tro(Class</pre>
5	<pre>tro(subClassExpression, [Object Data]AllValuesFrom(property<sub>1</sub> ...[Object Data]AllValuesFrom(property<sub>n</sub> [Object Data]MaxCardinality(1 PropertyExpression ClassExpression) ...),?x)</pre>	<pre>Forall ? And( tro(subCl ?x[tr(prop &gt; ?y<sub>2</sub>) ... ?y<sub>n-1</sub>[tr( tro(Class tro(Class</pre>
6	<pre>tro(A,?x)</pre>	<pre>?x[rdf:t</pre>

7	<code>tro([Object Data]IntersectionOf(ClassExpression<sub>1</sub> ... ClassExpression<sub>n</sub>), ?x)</code>	And (tro(C tro(Class
8	<code>tro(ObjectUnionOf(ClassExpression<sub>1</sub> ... ClassExpression<sub>n</sub>), ?x)</code>	Or (tro(Cl tro(Class
9	<code>tro([Object Data]OneOf(Individual<sub>1</sub> ... Individual<sub>n</sub>), ?x)</code>	Or ( ?x = tr(Indivi
10	<code>tro([Object Data]SomeValuesFrom(PropertyExpression ClassExpression)), ?x)</code>	Exists ? tro(Class
11	<code>tro(X, ?x, ?y)</code>	?x[tr(x) -
12	<code>tro(ObjectInverseOf(X), ?x, ?y)</code>	?y[tr(Prop
13	<code>tro([Object Data]HasValue(PropertyExpression value), ?x)</code>	tro(Prope
14	<code>tro( SubObjectPropertyOf(ObjectPropertyChain(PropertyExpression<sub>1</sub> ... PropertyExpression<sub>m</sub>) PropertyExpression<sub>0</sub>) )</code>	Forall ? (tro(Prop tro(Prope tro(Prope ... tro(Prope
15	<code>tro( Sub[Object Data]PropertyOf(PropertyExpression<sub>1</sub> PropertyExpression<sub>2</sub>) )</code>	Forall ? :- tro(P

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16	tro( Disjoint[Object Data]Properties(PropertyExpression <sub>1</sub> PropertyExpression <sub>2</sub> ) )	Forall ? And (tro(P tro(Prope
17	tro( InverseObjectProperties(PropertyExpression <sub>1</sub> PropertyExpression <sub>2</sub> ) )	Forall ? :- tro(P Forall ? :- tro(P
18	tro( Functional[Object Data]Property(PropertyExpression) )	Forall ? And (tro(P tro(Prope
19	tro( InverseFunctional[Object Data]Property(PropertyExpression) )	Forall ? And (tro(P tro(Prope
20	tro( IrreflexiveObjectProperty(PropertyExpression) )	Forall ? tro(Prope
21	tro( SymmetricObjectProperty(PropertyExpression) )	Forall ? tro(Prope
22	tro( AsymmetricObjectProperty(PropertyExpression) )	Forall ? And (tro(P tro(Prope
23	tro( TransitiveObjectProperty(PropertyExpression) )	Forall ? ?z) :- A tro(Prope

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24	tro( DatatypeDefinition(datatypeIRI DataRange) )	Forall ? tro(DataR Forall ? tr(dataty
25	tro( HasKey(subClassExpression PropertyExpression <sub>1</sub> ... PropertyExpression <sub>m</sub> ) )	Forall ? And (tro(s tro(subCl tro(Prope tro(Prope tro(Prope tro(Prope
26	tro( SameIndividual (Individual <sub>1</sub> Individual <sub>2</sub> ) )	tr(Indivi
27	tro( DifferentIndividuals (Individual <sub>1</sub> Individual <sub>2</sub> ) )	rif:error

Besides the embedding in the previous table, we also need an axiomatization of some of the aspects of the OWL DL semantics, e.g., separation between individual and datatype domains. This axiomatization is defined relative to an OWL vocabulary  $V$ , which includes all well-typed literals used in the rules, and a datatype map  $D$ , which includes all considered datatypes. In the table, for a given datatype  $d$ ,  $L2V(d)$  is the lexical-to-value mapping of  $d$ .

$R^{OWL}(V)$	=	<pre>merge({ (i) (Forall ?x (rif:error :- ?x[rdf:type -&gt; owl:Nothing]), (ii) Forall ?x (rif:error :- And(?x[rdf:type -&gt; rdfs:Literal] ?x[rdf:type -&gt; owl:Thing])), (iii) (Forall ?x (?x[rdf:type -&gt; owl:Thing] :- ?x[rdf:type -&gt; C])) for every class ID C, (iv) (Forall ?x (?x[rdf:type -&gt;</pre>
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		<pre> rdfs:Literal] :- ?x[rdf:type -&gt; D])) for every datatype ID D, (v) (Forall ?x ?y (?x[rdf:type -&gt; owl:Thing] :- ?x[P -&gt; ?y])) for every property ID P, (vi) (Forall ?x ?y (?y[rdf:type -&gt; owl:Thing] :- ?x[P -&gt; ?y])) for every object property ID P, (vii) (Forall ?x ?y (?y[rdf:type -&gt; rdfs:Literal] :- ?x[P -&gt; ?y])) for every data property ID P, (viii) (tr(i)[rdf:type -&gt; owl:Thing]) for every IRI i in V, (ix) (tr(s^^u)[rdf:type -&gt; u']) for every well-typed literal s^^u and datatype identifier u' in V such that L2V(D(u))(s) is in the value space of u', (x) (rif:error :- tr(s^^u)[rdf:type -&gt; u']) for every well-typed literal s^^u and datatype identifier u' in V such that L2V(D(u))(s) is not in the value space of u', (xi) (Forall ?x (?x[rdf:type -&gt; rdfs:Literal] :- ?x[rdf:type -&gt; Diri])) for every datatype in D with identifier <i>Diri</i>, (xii) "a"="b" :- rif:error}) </pre>
--	--	---

We call an OWL 2 RL ontology *O* *normalized* if it is the same as its normalization, i.e.,  $O = \text{tr}_N(O)$ .

The following lemma establishes faithfulness of the embedding.

**Normalized Combination Embedding Lemma** Given a datatype map *D* conforming with *T*, a [RIF-OWL DL-combination](#)  $C = \langle R, \{O_1, \dots, O_n\} \rangle$ , where  $\{O_1, \dots, O_n\}$  is an imports-closed set of normalized OWL 2 RL ontologies with vocabulary *V*, [RIF-OWL DL-entails](#) a DL-condition  $\varphi$  with respect to *D* iff  $\text{merge}(\{R, R^{\text{OWL-DL}}(V), \text{tr}_O(O_1), \dots, \text{tr}_O(O_n)\})$  [dl-entails](#)  $\varphi$ .

The following theorems establish faithfulness of the full embedding of RIF-OWL 2 RL combinations into RIF.

**Theorem** Given a datatype map *D* conforming with *T*, a [RIF-OWL DL-combination](#)  $C = \langle R, \{O_1, \dots, O_n\} \rangle$ , where  $\{O_1, \dots, O_n\}$  is an imports-closed set of OWL 2 RL ontologies with vocabulary *V*, [RIF-OWL DL-entails](#) a DL-condition formula  $\varphi$  with respect to *D* iff  $\text{tr}(\text{merge}(\{R, R^{\text{OWL-DL}}(V), \text{tr}_N(\text{tr}_N(O_1)), \dots, \text{tr}_N(\text{tr}_N(O_n))\}))$  [entails](#)  $\text{tr}(\varphi)$ .

**Theorem** Given a datatype map  $D$  conforming with  $T$ , a [RIF-OWL-DL-combination](#)  $\langle R, \{O_1, \dots, O_n\} \rangle$ , where  $\{O_1, \dots, O_n\}$  is an imports-closed set of OWL 2 RL ontologies with vocabulary  $V$ , is [owl-dl-satisfiable](#) with respect to  $D$  iff  $\text{tr}(\text{merge}(\{R, R^{\text{OWL-DL}}(V), \text{trO}(\text{trN}(O_1)), \dots, \text{trO}(\text{trN}(O_n))\}))$  does not entail `rif:error`.

## 10 Appendix: Change log (Informative)

Changes since the [3 July 2009 Working Draft](#).

In the definition of [common-RIF-RDF-interpretation](#), "RDF interpretation" was replaced with "Simple interpretation". The original reference to "RDF interpretation" was an error.

The notions RDFS-model, OWL DL-entailment, etc. have been renamed to RIF-RDFS-model, RIF-OWL DL-entailment, etc.

## 11 End Notes

**RDF URI References:** There are certain RDF URI references that are not IRIs (e.g., those containing spaces). It is possible to use such RDF URI references in RDF graphs that are combined with RIF rules. However, such URI references cannot be represented in RIF rules and their use in RDF is discouraged.

**Generalized RDF graphs:** Standard [RDF graphs](#), as defined in [\[RDF-Concepts\]](#), do not allow the use of literals in subject and predicate positions and blank nodes in predicate positions. The [RDF Core](#) working group has listed two [issues](#) questioning the restrictions that [literals may not occur in subject](#) and [blank nodes may not occur in predicate](#) positions in triples. Anticipating lifting of these restrictions in a possible future version of RDF, we use the more liberal notion of *generalized* RDF graph. We note that the definitions of interpretations, models, and entailment in the RDF semantics document [\[RDF-Semantics\]](#) also apply to such generalized RDF graphs.

We note that every standard RDF graph is a generalized RDF graph. Therefore, our definition of combinations applies to standard RDF graphs as well.

We note also that the notion of generalized RDF graphs is more liberal than the notion of RDF graphs used by [SPARQL](#); generalized RDF graphs additionally allow blank nodes and literals in predicate positions.